



SWAMI VIVEKANANDA SCHOOL OF

ENGINEERING & TECHNOLOGY

LECTURE NOTE

REFRIGERATION & AIR CONDITIONING

ER. ANIL KUMAR PANDA

Date: 09/08/2023

Refrigeration :-

It is the process of producing and maintaining low temperature for a storage space in compare to atmospheric temperature.

Refrigeration effect (RE, Q_c) :-

It is the amount of heat which is to be removed from storage space in order to produced and maintaining low temperature.

Unit of refrigeration :-

(i) It is the amount of heat is just to be removed from 1 ton of water at 0°C in order to convert into ice at 0°C in 24 hours.

(ii) The heat transperate corresponding to this process is defined as "ton of refrigeration" (TR) = 1TR

Since the latent heat of ice is 335 KJ/Kg , therefore, one ton of refrigeration,

$$1\text{TR} = 907 \times 335 \text{ Kg in } 24 \text{ hr}$$

$$= \frac{907 \times 335}{24 \times 60} = 211 \text{ KJ/min}$$

Coefficient of performance of Refrigeration system

Coefficient of performance (C.O.P) is the ratio of heat extracted in the refrigerator to the work done on the refrigerant.

It is also known as theoretical coefficient of performance

Mathematically,

$$\text{Theoretical C.O.P} = \frac{Q}{W}$$

\therefore Q = amount of heat extracted in refrigerator

W = work done on the refrigerant.

* The ratio of actual C.O.P to the theoretical C.O.P is known as Relative C.O.P

Mathematically,

$$\text{Relative C.O.P} = \frac{\text{Actual C.O.P}}{\text{Theoretical C.O.P}}$$

Ques Find the COP of refrigeration system if the work done input is 80 kJ/kg and refrigeration effect produced is 160 kJ/kg of refrigerant.

Soln: Given:

$$W = 80 \text{ kJ/kg}$$

$$Q_c = 160 \text{ kJ/kg}$$

We know that C.O.P of refrigeration system

$$\therefore \text{C.O.P of (refrigerant)} = \frac{Q_c}{W}$$

$$= \frac{160 \text{ kJ/kg}}{80 \text{ kJ/kg}}$$

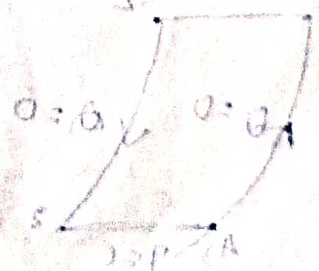
$$= 2$$

(Ans)

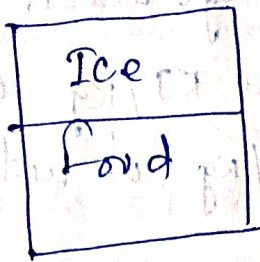
Date: 11/08/2023

Different type of refrigeration cycle:

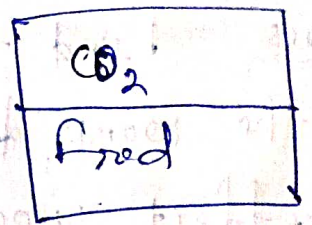
1. Ideal Refrigeration cycle
2. Ice Ref. cycle
3. Dry Ice Ref. cycle
4. Evaporative Ref. cycle (Indian Ref. system)
5. Expand Ref. cycle



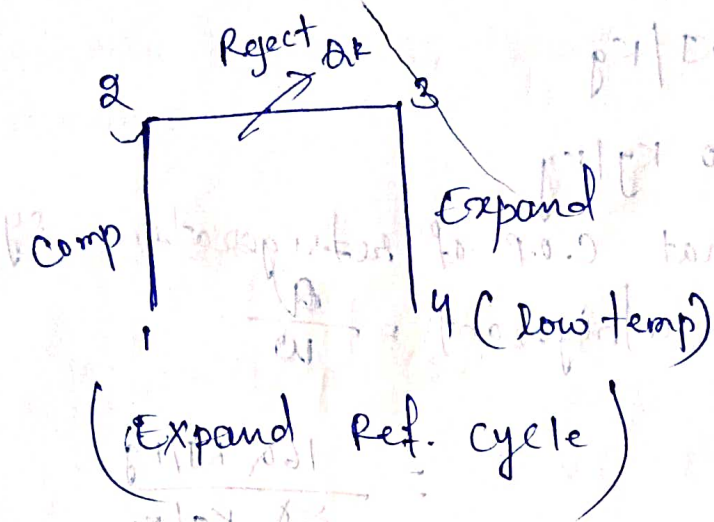
②



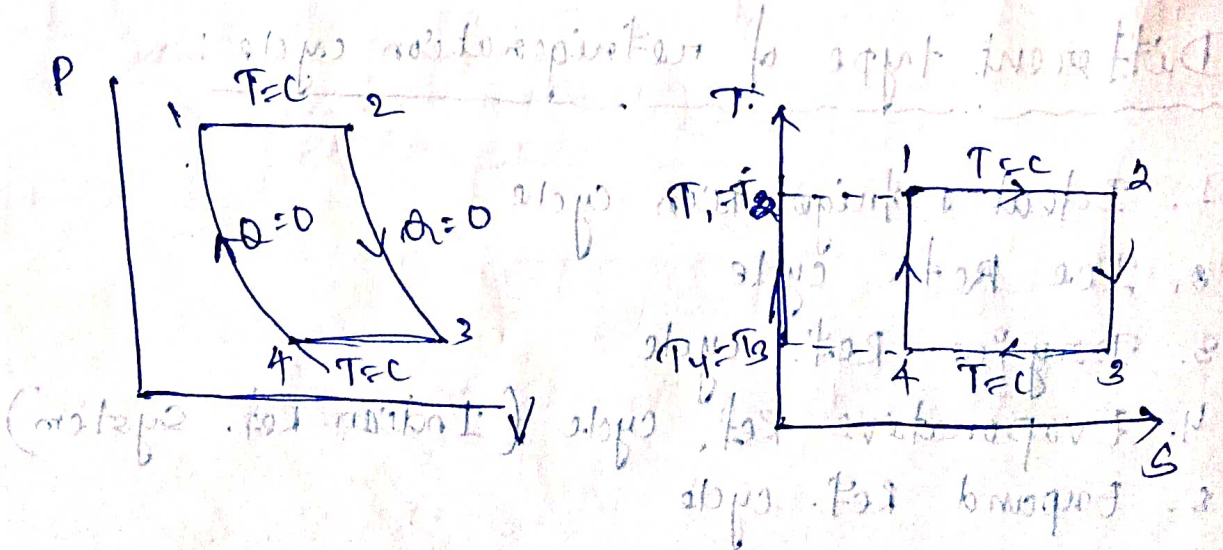
②



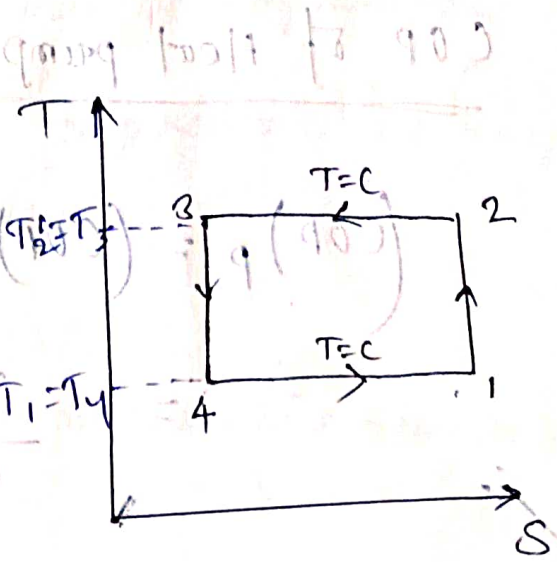
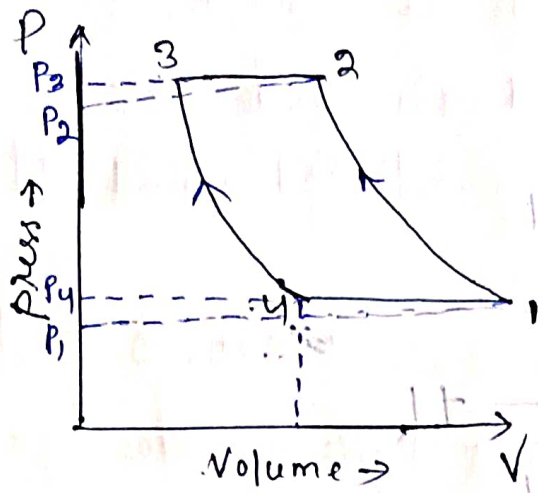
⑤



④ Ideal Ref. cycle :-
(Reverse Carnot cycle)



Dt: 18/08/2023



$$\frac{q_2}{q_1} = \frac{T_2}{T_1}$$

$$\frac{q_2}{q_1 - q_2} = \frac{T_2}{T_1 - T_2}$$

COP of reversed carnot cycle:-

$$(C.O.P)_R = \frac{\text{heat absorbed}}{\text{work done}}$$

$$= \frac{q_A}{(q_R - q_A)}$$

$$= \frac{q_{2-3}}{q_{2-3} - q_{4-1}}$$

$$= \frac{q_{2-3}}{q_{2-3} - q_{4-1}}$$

$$= \frac{T (s_2 - s_3)}{(T_2 - T_1)(s_2 - s_1)}$$

$$= \frac{T_1}{T_2 - T_1}$$

COP of Heat pump:-

$$(COP)_p = (COP)_R + 1$$

$$= \frac{T_2}{T_2 - T_1} + 1$$

$$= \frac{T_2}{T_2 - T_1}$$

COP of efficiency of a heat engine:-

$$(COP)_E = \frac{W_R}{Q_R}$$

$$= \frac{(T_2 - T_1)(S_2 - S_3)}{T_2(S_2 - S_3)}$$

$$= \frac{(T_2 - T_1)}{T_2}$$

$$= \frac{1}{(COP)_p}$$

COP of reversed Carnot cycle may be improve by

i. Decreasing the higher temperature (i.e. temp of ~~the~~ hot body T_2)

ii) Increasing the lower temperature (i.e. temperature of cold body T_1)

$$\frac{1}{\text{COP}} = \frac{1}{(900)} \quad \text{--- (iii)}$$

Ques: A machine working on a Carnot cycle operates between 305 K and 260 K . Determine the COP when it is operated as

(i) Refrigeration machine

(ii) Heat pump

(iii) Heat Engine

Given; $T_1 = 305\text{ K}$, $T_2 = 260\text{ K}$

(i) Refrigeration machine

$$(\text{COP})_R = \frac{260}{305 - 260} = \frac{260}{45} = 5.78$$

$$(ii) (COP)_p = \frac{T_a}{T_g - T_a}$$

$$= \frac{305}{305 - 260}$$

$$= \frac{61}{85} = 6.78$$

$$(iii) (COP)_E = \frac{1}{(COP)_p} = \frac{1}{6.78}$$

$$= \frac{100}{678} \times 100 = 0.147$$

Ques A Carnot refrigeration cycle absorbs heat at 270K rejects it at 300K

(i) Calculate the coefficient of performance of refrigeration cycle

(ii) If the cycle is absorbing 1130 kJ/min at 270K how many kJ of work is required per second

(iii) If the Carnot heat pump operates between the same temperature as the above refrigeration cycle, what is the COP

(iv) How many kJ per min will the heat pump deliver at 300K if heat absorbs 1130 kJ per minute at 270K

Solution:

Given: $T_1 = 270\text{K}$, $T_2 = 300\text{K}$

(i) C.O.P of refrigeration cycle

$$\begin{aligned}(\text{COP})_R &= \frac{T_1}{T_2 - T_1} \\ &= \frac{270\text{K}}{(300 - 270)\text{K}} \\ &= \frac{270}{30} = 9 \quad (\text{Ans})\end{aligned}$$

(ii) If cycle is absorbing 1130 kJ/min at 270K

$$Q_1 = 1130 \text{ kJ/min}$$

$$\begin{aligned}&= \frac{1130 \text{ kJ}}{60 \text{ sec}} = \frac{1130}{60} \\ &= 18.83 \text{ kJ/sec}\end{aligned}$$

We know that

$$(C.O.P)_R = \frac{Q_1}{W_1}$$

$$\Rightarrow 9 = \frac{18.883}{W_1}$$

$$\Rightarrow W_1 = \frac{18.883}{9}$$

$$= 2.1 \text{ KJ/sec (Ans)}$$

(iii)

C.O.P of heat pump

$$(C.O.P)_P = \frac{T_2}{T_2 - T_1}$$

$$= \frac{300}{300 - 270}$$

$$= \frac{300}{30}$$

$$= 10 \text{ (Ans)}$$

Q.14) We know that COP of heat pump

$$(C.O.P)_p = \frac{Q_2}{Q_2 - Q_1}$$

$$\Rightarrow 10 = \frac{Q_2}{Q_2 - 1130}$$

$$\Rightarrow 10 = \frac{Q_2}{Q_2 - 1130}$$

10Q₂ = 11300 = Q₂

$$\Rightarrow 10Q_2 - 11300 = Q_2$$

$$\Rightarrow 10Q_2 = Q_2 + 11300$$

$$\Rightarrow 10Q_2 - Q_2 = 11300$$

$$\Rightarrow 9Q_2 = 11300$$

$$\Rightarrow Q_2 = \frac{11300}{9} = 1255.6 \text{ kJ/min}$$

(Ans)

We know that COP of refrigerator

$$(C.O.P)_r = \frac{Q_1}{Q_2 - Q_1}$$

$$\Rightarrow \frac{11}{10} = \frac{Q_1}{Q_2 - Q_1}$$

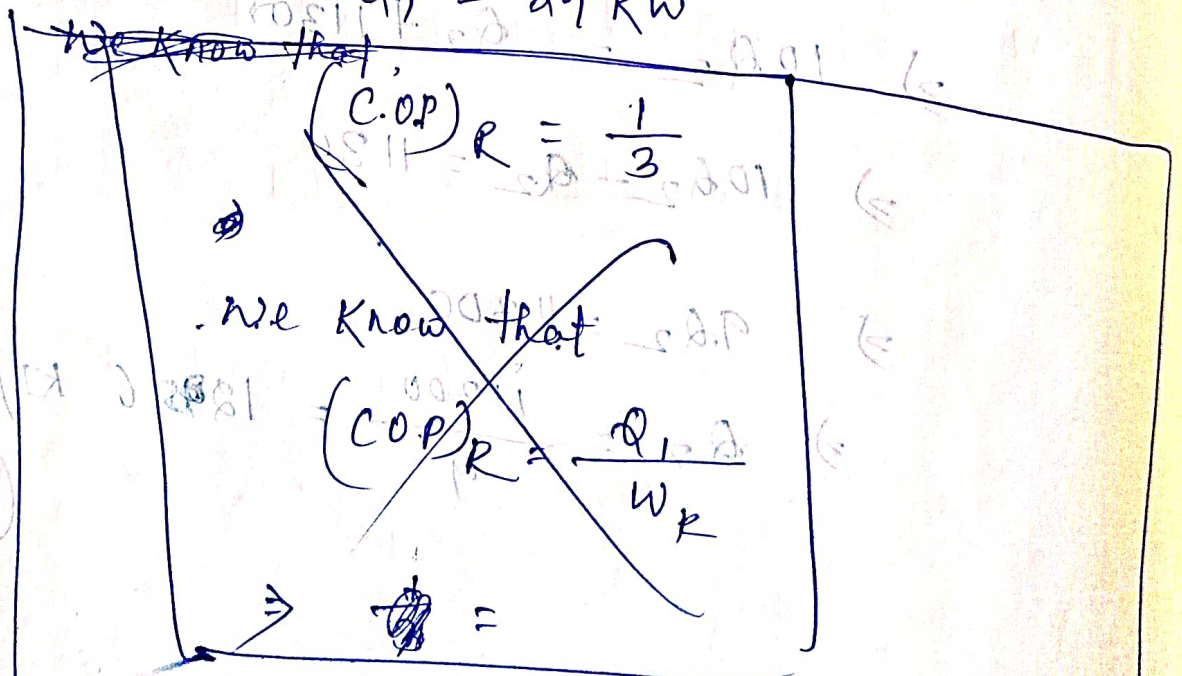
Ques A cold storage is to be maintained at -5°C while the surrounding one at 35°C . The heat rejects from the surroundings in to the cold storage is estimated to be 29 kW . The actual cop of refrigeration plant is $\frac{1}{3}$ of an ideal plant working between the same temperature. Find the power required to drive the plant

Soln

Given; $T_1 = -5^{\circ}\text{C} = -5 + 273\text{K} = 268\text{K}$

$T_2 = 35^{\circ}\text{C} = 35 + 273\text{K} = 308\text{K}$

$Q_1 = 29\text{ kW}$



We know that COP of refrigeration

~~$(\text{C.O.P})_R = \frac{Q_1}{W_R}$~~

~~$\Rightarrow \frac{T_1}{T_2 - T_1} = \frac{29}{W_R}$~~

Putting the value of $(COP)_I$ in eqn (1) we get

$$(COP)_A = \frac{6.7}{3} = 2.233 \quad (\text{Ans})$$

$$\therefore (COP)_A = \frac{Q_1}{W_R}$$

$$\Rightarrow 2.233 = \frac{29 \text{ kW}}{W_R}$$

$$\Rightarrow W_R = \frac{29 \text{ kW}}{2.233}$$

$$= 12.98 \text{ kW} \quad (\text{Ans}) \quad (i)$$

$$(COP)_A = \frac{T_1}{T_1 - T_2}$$

$$2.233 = \frac{328}{328 - 308}$$

$$(iii) \quad \frac{328}{20} = 16.4$$

(iii) Power required

We know that

$$(COP)_R = \frac{Q_1}{W_R}$$

Dt: 19/08/2023

Ques: A refrigeration system operates on the reverse Carnot cycle. The higher temperature of the refrigerant in the system is 35°C and the lower temperature is -15°C . The capacity is to be 12 tonnes determine

- (i) COP
- (ii) Heat rejected from the system per hour.
- (iii) Power required

Solution Given; $T_H = T_2 = 35^{\circ}\text{C} = 35 + 273 = 308\text{K}$
 $T_L = T_1 = -15^{\circ}\text{C} = -15 + 273 = 258\text{K}$
 $Q_1 = 12\text{TR} = 12 \times 210 = 2520 \text{ kJ}$

(i) COP of refrigeration system

$$\begin{aligned}(\text{COP})_R &= \frac{T_1}{T_2 - T_1} \\ &= \frac{258\text{K}}{(308 - 258)\text{K}} \\ &= \frac{258}{50} = 5.16 \quad (\text{Ans})\end{aligned}$$

(iii) ~~Heat~~ Power required

We know that

$$(\text{COP})_R = \frac{Q_1}{W_R}$$

$$\Rightarrow 5.16 = \frac{2520}{W_R}$$

$$\Rightarrow W_R = \frac{2520 \text{ KJ/min}}{5.16}$$

$$= 488.3 \text{ KJ/min (Ans)}$$

$$= 8.13 \text{ KJ/sec}$$

(ii) Heat rejected from the system per hour

We know that

$$Q_2 = Q_1 + W_R$$

$$= 2520 + 488.3 \text{ KJ/min}$$

$$= 3008.3 \text{ KJ/min}$$

$$= \frac{3008.3 \text{ KJ/min} \times 60}{60}$$

$$= 3008.3 \times 60 \text{ KJ/hr}$$

$$= 180498 \text{ KJ/hr (Ans)}$$

Ques: The capacity of a refrigerator is 200 TR when working between -6°C and 25°C . Determine the mass of ice produced per day from water at 25°C . Also find the power required to drive the unit. Assume that the cycle operates on reversed Carnot cycle and latent heat of ice 335 kJ/kg .

Solution: Given

The capacity of refrigerator = 200 TR = $200 \times 210 \text{ kJ/min}$

Latent heat of ice = 335 kJ/kg

$$T_L = T_1 = -6^{\circ}\text{C} = -6 + 273 \text{ K} = 267 \text{ K}$$

$$T_H = T_2 = 25^{\circ}\text{C} = 25 + 273 \text{ K} = 308 \text{ K}$$

$$\text{Latent heat of ice} = 335 \text{ kJ/kg}$$

Heat removed from 1 kg of water at 25°C to 0°C

$$= \text{mass} \times \text{specific heat} \times \text{rising temperature} + \text{latent heat}$$

$$= 1000 \times 4.187 (25 - 0) + 335$$

$$= 439.5 \text{ kJ/kg}$$

Mass of ice produced per minute

$$= \frac{\text{Heat capacity}}{\text{Heat removed}}$$

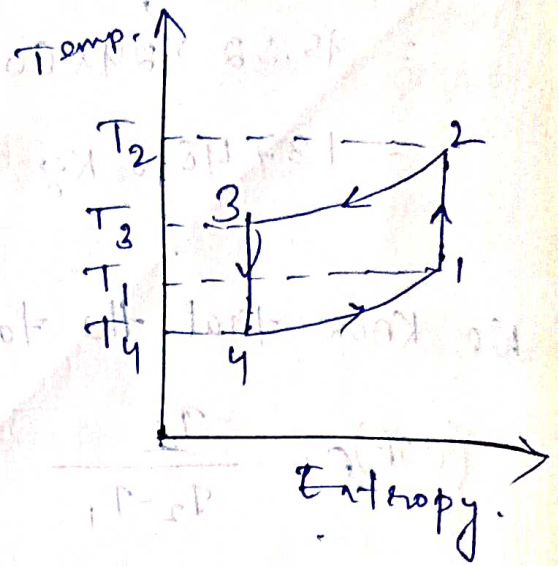
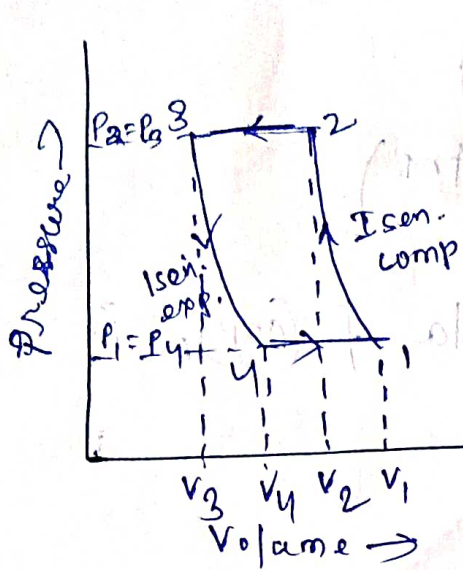
$$= \frac{42000 \text{ kJ/min}}{439.5 \text{ kJ/kg}}$$

$$= 95.56 \text{ kg/min}$$

$$= 95.56 \text{ kg/min}$$

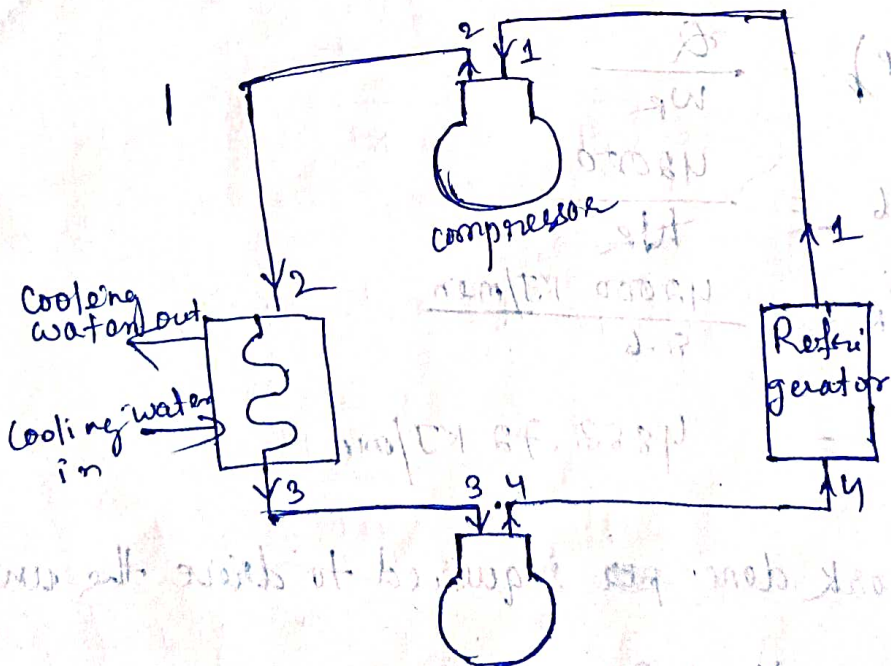
$$= 95.56 \text{ kg/min}$$

Bell-Coleman refrigeration cycle



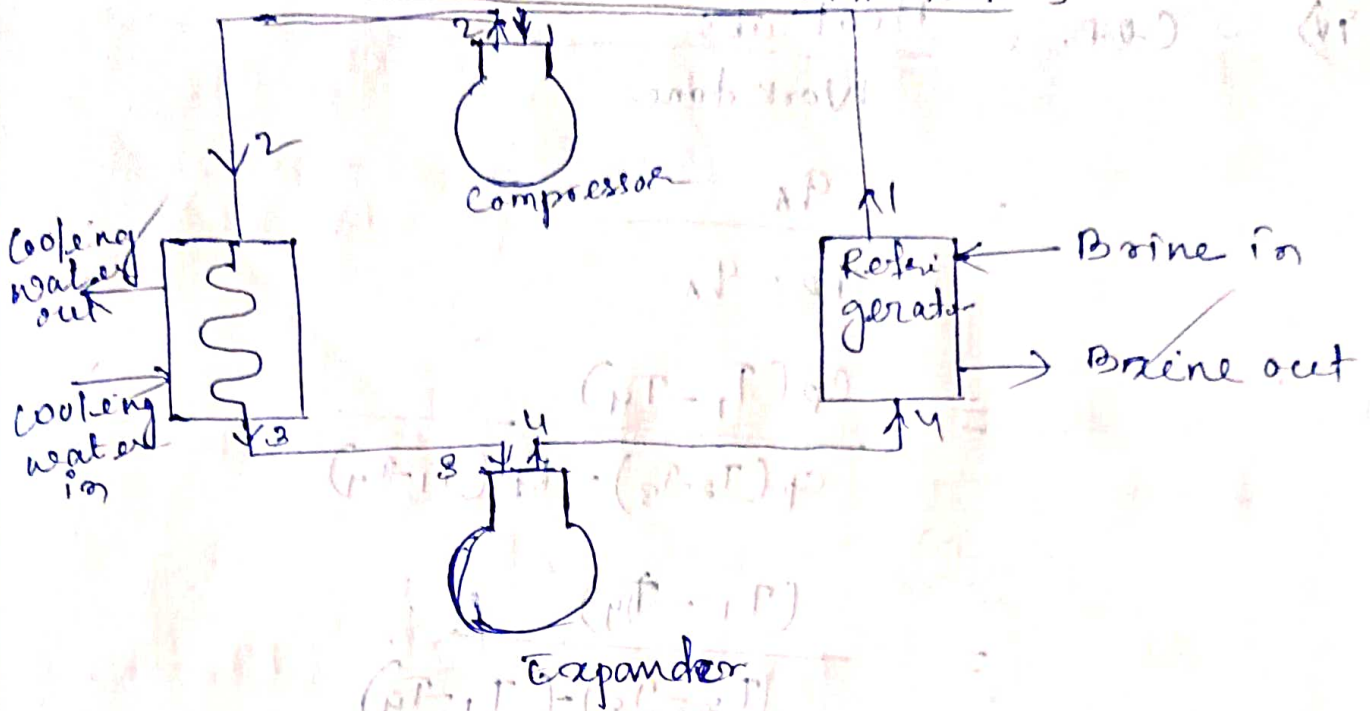
a) P-v diagram

b) T-s diagram



OPEN CYCLE AIR BELL-COLEMAN REF.

CLOSED CYCLE AIR BEER-COLEMAN REF



Date: 23/08/2023

(i) The heat rejected by the air during constant pressure per kg of air

$$Q_R = Q_{2-3} = C_p (T_2 - T_3)$$

(ii) The heat abs. by air / heat extracted from ref / the refrigerating effect produced during constant pressure expansion per kg of air is

$$Q_A = Q_{4-1} = C_p (T_1 - T_4)$$

(iii) The work done during the cycle per kg of air

= Heat rejected - Heat absorbed

$$= Q_R - Q_A = C_p (T_2 - T_3) - C_p (T_1 - T_4)$$

iv)

$$\text{C.O.P.} = \frac{\text{Heat abs}}{\text{Work done}}$$

$$= \frac{q_A}{q_R - q_A}$$

$$= \frac{C_p(T_1 - T_4)}{C_p(T_2 - T_3) - C_p(T_1 - T_4)}$$

$$= \frac{(T_1 - T_4)}{(T_2 - T_3) - (T_1 - T_4)}$$

$$= \frac{T_4 \left(\frac{T_1}{T_4} - 1 \right)}{T_3 \left(\frac{T_2}{T_3} - 1 \right) - T_4 \left(\frac{T_1}{T_4} - 1 \right)}$$

We know that, for isentropic comp. process

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}} \quad \text{--- (ii)}$$

Similarly, for isentropic expansion process

$$\frac{T_3}{T_4} = \left(\frac{P_3}{P_4} \right)^{\frac{\gamma-1}{\gamma}} \quad \text{--- (iii)}$$

Since $P_2 = P_3$ and $P_1 = P_4$ there are eqn (ii) and (iii)

$$\left(\frac{T_2}{T_1} \right)^{\frac{\gamma}{\gamma-1}} = \left(\frac{T_3}{T_4} \right)^{\frac{\gamma}{\gamma-1}} \quad \text{or} \quad \frac{T_2}{T_3} = \frac{T_1}{T_4} \quad \text{--- (iv)}$$

Now substituting the value in eqn (1)

$$C.O.P = \frac{T_4 \left(\frac{T_3}{T_4} - 1 \right)}{T_3 \left(\frac{T_2}{T_3} - 1 \right) - T_4 \left(\frac{T_1}{T_4} - 1 \right)}$$

$$= \frac{T_4 \left(\frac{T_3}{T_4} - 1 \right)}{T_3 \left(\frac{T_1}{T_4} - 1 \right) - T_4 \left(\frac{T_1}{T_4} - 1 \right)}$$

$$= \frac{T_4 \left(\frac{T_3}{T_4} - 1 \right)}{T_3 - T_4}$$

$$= \frac{T_4 \left(\frac{T_3}{T_4} - 1 \right)}{T_3 - T_4}$$

$$= \frac{1}{\left(\frac{T_3}{T_4} - 1 \right) \frac{T_3}{T_4} - \left(\frac{T_1}{T_4} - 1 \right)}$$

Let $\frac{P_2}{P_1} = r_p$: compression ratio or expansion ratio.

~~*~~ Some times compression and expansion process take place according to the law of $PV = \text{constant}$.

i) We know that work done by compressor during the process 1-2 for kg of air

$$W_c = \frac{n}{n-1} (P_2 V_2 - P_1 V_1) = \frac{n}{n-1} (RT_2 - RT_1)$$

$\left(\frac{P_2 V_2}{P_1 V_1} \right)^{\frac{n-1}{n}} = \frac{T_2}{T_1}$
 $\left(\because PV = RT \right)$

ii) Work done by the expander during the process 3-4 per kg of air

$$W_E = \frac{n}{n-1} (P_3 V_3 - P_4 V_4) = \frac{n}{n-1} (RT_3 - RT_4)$$

$P V = RT = \frac{n}{n-1} \times R (T_3 - T_4)$

iii) Net work done during complete cycle per kg of air

$$W = W_c - W_E = \frac{n}{n-1} (RT_2 - RT_1) - \frac{n}{n-1} (RT_3 - RT_4)$$

iv) C.O.P = $\frac{\text{Heat absorbed}}{\text{work done}}$

$$\frac{C_p (T_1 - T_4)}{\frac{n}{n-1} \times R [(T_2 - T_1) - (T_3 - T_4)]}$$

We know that $R = C_p - C_v$
 $C_p = C_v (1 + \gamma)$

we know that work done per cycle per kg of air is $W = \frac{n}{n-1} R (T_2 - T_1 - T_3 + T_4)$

Heat absorbed per kg of air is $Q_1 = C_p (T_1 - T_4)$

C.O.P = $\frac{Q_1}{W} = \frac{C_p (T_1 - T_4)}{\frac{n}{n-1} R (T_2 - T_1 - T_3 + T_4)}$

* Substituting

1 The value of R in equation (vi)

$$C.O.P = \frac{C_p (\tau_1 - \tau_4)}{\frac{n}{n-1} \times R \left[(\tau_2 - \tau_1) - (\tau_3 - \tau_4) \right]}$$

$$= \frac{C_p (\tau_1 - \tau_4)}{\frac{n}{n-1} \times (\gamma - 1) C_v \left[(\tau_2 - \tau_1) - (\tau_3 - \tau_4) \right]}$$

$$= \frac{\gamma (\tau_1 - \tau_4)}{\frac{n}{n-1} \times (\gamma - 1) \left[(\tau_2 - \tau_1) - (\tau_3 - \tau_4) \right]}$$

$$= \frac{\gamma (\tau_1 - \tau_4)}{\frac{n}{n-1} \times \left(\frac{\gamma - 1}{\gamma} \right) \left[(\tau_2 - \tau_1) - (\tau_3 - \tau_4) \right]}$$

$$C.O.P = \left(\frac{n-1}{n} \right) \times \left(\frac{\gamma}{\gamma-1} \right) \times \frac{\tau_4}{\tau_3 - \tau_4}$$

Note:

(1) In this case the value of τ_2 and τ_4 are to be obtained from the following relations

$$\frac{\tau_2}{\tau_1} = \left(\frac{P_2}{P_1} \right)^{\frac{n-1}{n}} \quad \text{or} \quad \frac{\tau_3}{\tau_4} = \left(\frac{P_3}{P_4} \right)^{\frac{n-1}{n}}$$

2. for Isentropic compression or expansion $\eta = \gamma$
 therefore, the equation (vii) may be written as

$$\text{COP} = \frac{T_1 - T_4}{\left[(T_2 - T_3) - (T_1 - T_4) \right]}$$

$$\left[(T_2 - T_3) - (T_1 - T_4) \right] = (T_1 - T_4) \left[\left(\frac{P_2}{P_1} \right)^{\frac{\gamma}{\gamma-1}} - 1 \right]$$

Date: 24/08/2023

Ques: In a refrigeration plant working on Bell-Coleman cycle, air is compressed to 5 bar from 1 bar. Its initial temperature is 10°C after compression the air is cooled upto 20°C in a cooler before expanding that to a pressure of one bar. determine the theoretical COP of the plant and Net refrigeration effect

Take $C_p = 1.005 \text{ kJ/kgK}$, $C_v = 0.718 \text{ kJ/kgK}$

Soluⁿ: Given; $P_1 = P_4 = 1 \text{ bar}$,

$$P_2 = P_3 = 5 \text{ bar}$$

$$T_1 = 10^\circ\text{C} = 10 + 273 \text{ K} = 283 \text{ K}$$

$$T_3 = 20^\circ\text{C} = 20 + 273 = 293 \text{ K}$$

$$\left(\frac{P_2}{P_1} \right)^{\frac{\gamma}{\gamma-1}} = \frac{T_2}{T_1} \Rightarrow \frac{5}{1} = \frac{T_2}{283}$$

$$T_2 = 1.005 \text{ kJ/kgK}$$

$$c_v = 0.718 \text{ kJ/kg K}$$

We know that $\gamma = \frac{c_p}{c_v} = \frac{1.005}{0.718} = 1.4$

(i) The theoretical COP of the plant

$$\text{COP} = \frac{T_4}{T_3 - T_4}$$

We know that, for isentropic process

$$\left(\frac{P_3}{P_4}\right)^{\frac{\gamma-1}{\gamma}} = \frac{T_3}{T_4}$$

$$\Rightarrow \left(\frac{5}{1}\right)^{0.286} = \frac{293}{T_4}$$

$$\Rightarrow T_4 = \frac{293}{(5)^{0.286}} = 185 \text{ K}$$

$$\text{COP} = \frac{T_4}{T_3 - T_4} = \frac{185}{293 - 185} = 1.713 \text{ Ans}$$

ii) Net refrigeration effect

$$q_{A1} = q_{4-1} = c_p(T_1 - T_4)$$

$$= 1.005 \left(283 - \left(\frac{293}{5}\right) \right)$$

$$= 98.5 \text{ kJ/kg (Ans)}$$

Ques A refrigerator working on Bell-Coleman cycle operates between pressure limit of 1.05 bar and 8.5 bar. Air is drawn from the cold chamber at 10°C compressed and then it is cooled to 30°C before entering the expansion cylinder. The expansion & compression follows the law of $PV^{1.3} = \text{constant}$. Determine the theoretical COP of the system.

Soln Given data

$$P_1 = P_4 = 1.05 \text{ bar}$$

$$P_2 = P_3 = 8.5 \text{ bar}$$

$$T_1 = 10^\circ\text{C} = 10 + 273 \text{ K} = 283 \text{ K}$$

$$T_3 = 30^\circ\text{C} = 30 + 273 \text{ K} = 303 \text{ K}$$

$$PV^{1.3} = \text{const}$$

$$n = 1.3$$

Let, T_2 and T_4 = Temp. at the end of compression and expansion respectively.

Since, the compression & expansion follows the law $PV^{1.3} = c$, therefore

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{n-1}{n}} = \left(\frac{8.5}{1.05} \right)^{\frac{1.3-1}{1.3}} = 1.62$$

$$\therefore \frac{T_2}{1} = T_1 \times 1.62 = 283 \times 1.62 = 458.5 \text{ K}$$

Similarly,

$$\frac{T_3}{T_4} = \left(\frac{P_3}{P_4} \right)^{\frac{n-1}{n}} = \left(\frac{8.5}{1.05} \right)^{\frac{1.3-1}{1.3}} = 1.62$$

$$\therefore T_4 = \frac{T_3}{1.62} = \frac{303}{1.62} = 187 \text{ K}$$

We know that theoretical coefficient of performance

$$\text{C.O.P} = \frac{(T_1 - T_4)^{0.1}}{\frac{n}{n-1} \times \frac{(\gamma-1)}{\gamma} \times [(T_2 - T_3) - (T_1 - T_4)]}$$

$$= \frac{(283 - 187)}{\frac{1.3}{1.3-1} \times \frac{1.4-1}{1.4} \times [(458.5 - 303) - (283 - 187)]}$$

(taking $\gamma = 1.4$)

$$= \frac{96}{1.24 \times 59.5} = 1.3 \text{ Ans}$$

Ques The atmospheric air at pressure 1 bar and temp -5°C is drawn in the cylinder of the compressor of Bell-Coleman cycle. It is compressed isentropically to a pressure of 5 bar. In the cooler, the compressed air is cooled to 15°C , pressure remaining the same. It is then expanded to a pressure of 1 bar in an expansion cylinder, from where it is passed to the cold chamber. Find
 (i) The work done per kg of air, (ii) COP of the plant

For air assume law for expansion $p v^{1.2} = C$ & for compⁿ $p v^{1.4} = C$ and $C_p = 1 \text{ kJ/kgK}$

Soln Given data;

$$P_1 = P_4 = 1 \text{ bar}$$

$$P_2 = P_3 = 5 \text{ bar}$$

$$T_1 = -5^\circ\text{C} = -5 + 273 = 268 \text{ K}$$

$$T_3 = 15^\circ\text{C} = 15 + 273 = 288 \text{ K}$$

$$n = 1.2, \quad \gamma = 1.4$$

$$C_p = 1 \text{ kJ/kgK}$$

Let T_2 and T_4 = Temperature at the end of
Compression & expansion

Since, the compression follow the law $PV^\gamma = c$
therefore,

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}} = \left(\frac{5}{1}\right)^{\frac{1.4-1}{1.4}} = (5)^{0.286} = 1.585$$

$$\therefore T_2 = T_1 \times 1.585 = 424.8 \text{ K}$$

Similarly, the expansion follows the law $PV^\gamma = c$

therefore,

$$\frac{T_3}{T_4} = \left(\frac{P_3}{P_4}\right)^{\frac{\gamma-1}{\gamma}}$$

$$\Rightarrow \frac{288}{T_4} = \left(\frac{5}{1}\right)^{\frac{1.4-1}{1.4}}$$

$$T_4 = \frac{288}{(5)^{\frac{1}{3.86}}} = 220\text{K}$$

1. Work done per kg of air

We know that the work done by compressor 1-2

$$W_c = \frac{\gamma}{\gamma-1} \times R (T_2 - T_1)$$

$$= \frac{1.4}{1.4-1} \times 0.287 (424.8 - 288) \quad \therefore (\text{Take } R = 0.287)$$

$$= 159 \text{ KJ/Kg}$$

and work done by expander during the process 3-4 per kg of air

$$W_e = \frac{\eta}{\eta-1} \times R (T_3 - T_4)$$

$$= \frac{1.2}{1.2-1} \times 0.287 \times (288 - 220)$$

$$= 118.3 \text{ KJ/Kg}$$

\therefore Net work done by the system per kg of air

$$W = W_c - W_e$$

$$= 159 - 118.3 = 40.7 \text{ KJ/Kg} \quad \underline{\underline{\text{Ans}}}$$

2. - COP of the plant

$$\text{C.O.P} = \frac{C_p (T_1 - T_4)}{W} = \frac{48}{40.7}$$

$$= 1.18 \quad \underline{\underline{\text{Ans}}}$$

Ques: Refrigerator using Carnot cycle requires 1.25 kW per tonne of refrigeration to maintain a temperature of -30° . Find (i) COP of Carnot refrigerator, (ii) temperature at which heat is rejected, (iii) Heat rejected per tonne of refrigeration.

Soln Given data:

$$W_R = 1.25 \text{ kW} = 1.25 \text{ kJ/sec} = 1.25 \times 60 = 75 \text{ kJ/min}$$

$$T_1 = -30^\circ\text{C} = -30 + 273 = 243 \text{ K}$$

We know that heat extracted from the cold body

$$Q_1 = 210 \text{ kJ/min}$$

(i) COP of Carnot refrigerator

We know that

$$(\text{C.O.P})_R = \frac{Q_1}{W_R}$$

$$= \frac{210}{75} = 2.8$$

Ans

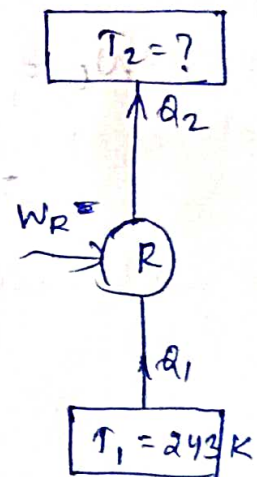
(ii) Temperature at which heat is rejected

We know that,

$$(\text{C.O.P})_R = \frac{T_1}{T_2 - T_1}$$

$$\Rightarrow 2.8 = \frac{243}{T_2 - 243}$$

$$\Rightarrow T_2 - 243 = \frac{243}{2.8}$$



$$\Rightarrow T_2 = \frac{243}{2.8} + 243 \quad \text{Ans (i)}$$

$$= 329.7 \text{ K} = 56.7^\circ \text{C} \quad \underline{\text{Ans}}$$

(iii) Heat rejected per tonne of refrigeration

$$Q_2 = W_R + Q_1$$

$$= 75 + 210 = 285 \text{ kJ/min} \quad \underline{\text{Ans}}$$

Ques A refrigeration system working on Bell Coleman receives air from cold chamber at -5°C and compress it from 1 bar to 4.5 bar. The compressed air is then cooled to a temperature of 27°C before it is expanded in the expander. Calculate COP of the system when expansion and compression are

(i) Isentropic

(ii) Follow the law $PV^{1.25} = C$

Soln Given data;

$$T_1 = -5^\circ \text{C} = -5 + 273 \text{ K} = 268 \text{ K} \quad \text{Ans (ii)}$$

$$T_3 = 27^\circ \text{C} = 27 + 273 = 300 \text{ K}$$

$$P_1 = P_4 = 1 \text{ bar}$$

$$P_2 = P_3 = 4.5 \text{ bar}$$

Let, T_2 and T_4 = Temperature at end of compression & expansion respectively.

(i) COP of the system when compression and expansion are isentropic

We know that

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}} = \left(\frac{4.5}{1}\right)^{\frac{1.4-1}{1.4}} = (4.5)^{\frac{0.4}{1.4}} = 1.4$$

$$\Rightarrow T_2 = T_1 \times 1.4 = 268 \times 1.4 = 375.2 \text{ K}$$

and,

$$\frac{T_3}{T_4} = \left(\frac{P_3}{P_4}\right)^{\frac{\gamma-1}{\gamma}} = \left(\frac{4.5}{1}\right)^{\frac{1.4-1}{1.4}} = 1.4$$

$$\Rightarrow T_4 = \frac{T_3}{1.4} = \frac{310}{1.4} = 221.4 \text{ K}$$

$$\text{COP} = \frac{1}{\left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}} - 1} = \frac{1}{(4.5)^{\frac{0.4}{1.4}} - 1} = 1.86 \quad \text{Ans}$$

(ii) COP of the system when follow the law $PV^{1.25} = C$

We know that

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{n-1}{n}} = \left(\frac{4.5}{1}\right)^{\frac{1.25-1}{1.25}} = (4.5)^{\frac{0.25}{1.25}} = 1.35$$

$$\Rightarrow T_2 = 1.35 \times T_1 = 1.35 \times 268 = 361.8 \text{ K}$$

and, $\frac{T_2}{T_4} = \left(\frac{P_2}{P_4}\right)^{\frac{\gamma-1}{\gamma}} = (4.5)^{\frac{1.25}{1.25}} = 1.25$

$\Rightarrow T_4 = \frac{T_2}{1.25} = \frac{310}{1.25} = 248 \text{ K}$

\therefore COP is $\left(\frac{\gamma-1}{\gamma}\right) \left(\frac{T_1}{T_2-1}\right) \times \frac{T_4}{T_2-T_4}$

$\frac{1.25-1}{1.25} \times \frac{1.4}{1.4-1} \times \frac{248}{310-248}$

and, $\frac{1.25-1}{1.25} \times \frac{1.4}{1.4-1} \times \frac{248}{310-248}$

and, $\frac{1.25-1}{1.25} \times \frac{1.4}{1.4-1} \times \frac{248}{310-248}$

and, $\frac{1.25-1}{1.25} \times \frac{1.4}{1.4-1} \times \frac{248}{310-248}$

and, $\frac{1.25-1}{1.25} \times \frac{1.4}{1.4-1} \times \frac{248}{310-248}$

and, $\frac{1.25-1}{1.25} \times \frac{1.4}{1.4-1} \times \frac{248}{310-248}$

Ques A dense air machine operates on reverse Brayton cycle and is required for a capacity of 10 TR. The cooler pressure is 4.2 bar and refrigerator pressure is 1.4 bar. The air is cooled in the cooler at a temperature of 50°C and the temperature of air at inlet to compressor is -20°C . Determine for the ideal cycle: 1. COP; 2. mass of air circulated per minute; 3. theoretical piston displacement of compressor; 4. theoretical piston displacement of expander; and 5. net power per ton of refrigeration

Soln; Given data;

$$Q = 10 \text{ TR}$$

$$P_2 = P_3 = 4.2 \text{ bar}$$

$$P_1 = P_4 = 1.4 \text{ bar}$$

$$T_3 = 50^\circ\text{C} = 50 + 273 = 323 \text{ K}$$

$$T_1 = -20 + 273 = 253 \text{ K}$$

Let, T_2 and T_4 = temperature at end of compression

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}}$$

$$\Rightarrow \frac{T_2}{253} = \left(\frac{4 \cdot 2}{1.4} \right)^{\frac{1.4-1}{1.4}} = 1.369$$

$$\Rightarrow T_2 = 1.369 \times 253 = 346 \text{ K}$$

Similarly,

$$\frac{T_3}{T_4} = \left(\frac{P_3}{P_4} \right)^{\frac{\gamma-1}{\gamma}}$$

$$\Rightarrow \frac{323}{T_4} = \left(\frac{4 \cdot 2}{1.4} \right)^{\frac{1.4-1}{1.4}} = 1.369$$

$$\Rightarrow T_4 = \frac{323}{1.369} = 236 \text{ K}$$

We know that,

$$\begin{aligned} \text{C.O.P} &= \frac{T_1 - T_4}{(T_2 - T_3) - (T_1 - T_4)} \\ &= \frac{(253 - 236)}{(346 - 323) - (253 - 236)} \\ &= 2.83 \quad \text{Ans} \end{aligned}$$

$$\text{(ii) } m_a = \frac{\text{Heat extracted/min}}{\text{Heat extracted/kg air}} \quad \text{Ans}$$

$$= \frac{2100 \text{ kJ/min}}{17}$$

We know that,

$$\text{Heat extracted } q_{\text{kg}} = c_p (T_1 - T_2)$$

$$17 \text{ kJ/kg} = 17 (253 - 236)$$

$$= 17 \text{ kJ/kg}$$

and $Q = 10 \text{ TR} = 10 \times 210 = 2100 \text{ kJ/min}$

$$m_a = \frac{2100 \text{ kJ/min}}{17 \text{ kJ/kg}}$$

$$= 123.5 \text{ kg/min}$$

Ans

(iii) Theoretical piston displacement of compressor per min

$$V_1 = \frac{m_a R_a T_1}{P_1}$$

$$= \frac{123.5 \times 0.287 \times 253}{1.4 \times 10^5 \text{ N/m}^2}$$

$$= 64.0 \text{ m}^3$$

(iv) $V_2 =$ Theoretical piston displacement of expander per min.

We know that $\gamma = 1$ i.e. constant pressure

$$\frac{V_4}{T_4} = \frac{V_1}{T_1}$$

$$\Rightarrow \frac{V_4}{236} = \frac{64}{253}$$

$$\Rightarrow V_4 = \frac{64 \times 236}{253} = 60.2 \text{ m}^3$$

(v) Net power per tonne of refrigeration.

We know that net work done on refrigerating machine per min.

$$= m a (\text{Heat rejected} - \text{Heat absorbed})$$

$$= m a \times c_p [(T_2 - T_3) - (T_1 - T_4)]$$

$$= 123.5 \times 1 [(346 - 323) - (253 - 236)]$$

$$= 741 \text{ kJ/min}$$

$$\text{Net power of refrigeration machine} = 741/60 \text{ kW}$$

$$= 12.35 \text{ kW}$$

$$\text{Net power per tonne of ref.} = 12.35/10 = 1.235$$

KW/TR

Merit of Air refrigeration system :-

- (i) The air is available (easily) and there is no cost of refrigerant.
- (ii) The air is non-toxic and ~~non~~ inflammable.
- (iii) The leakage of air is small, amount is tolerable.
- (iv) Since the main compressor is employed for the compressed air sources, therefore is no problem for space for extra compressor.
- (v) The air is light in weight per tonne of refrigerant.
- (vi) The chilled air is directly used for cooling there by eliminating the cost of separate evaporator.
- (vii) Since the pressure in the whole system is quite low therefore the piping, ducting etc are quite simple to design, fabricate and maintain.

Demerits of air refrigeration system :-

- (i) It has low coefficient of performance (C.O.P).
- (ii) The rate of air circulation is relatively large.

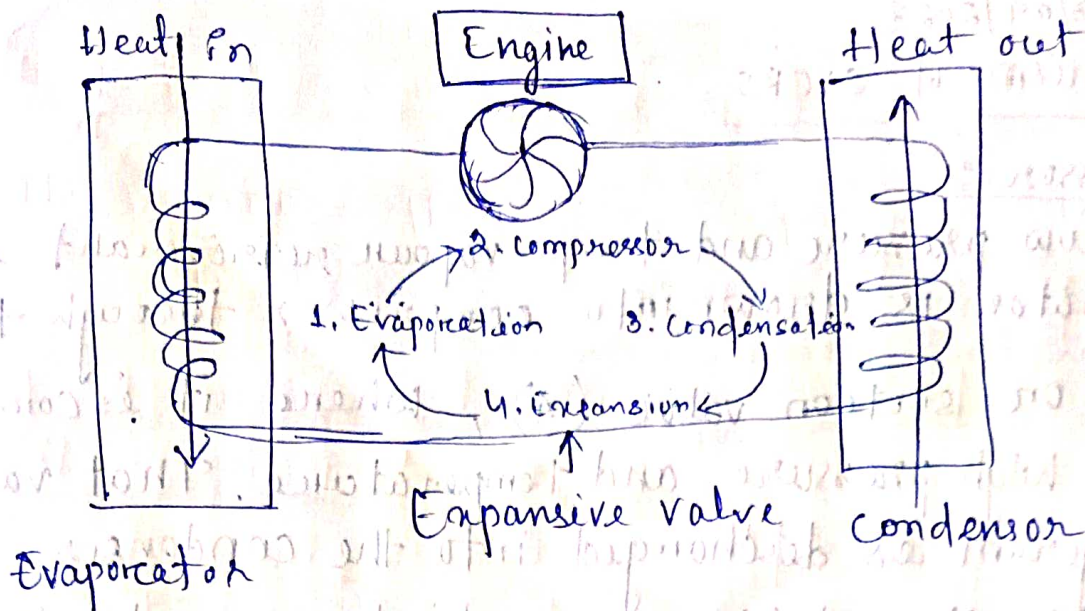
Methods of Air Ref. System

The various methods of air refrigeration ^{systems} used for aircrafts these days are the follows.

1. Simple air cooling system
2. Simple air evaporative cooling system
3. Boot strap air cooling system
4. Boot strap air evaporative cooling system
5. Reduced ~~air~~ ambient air cooling system
6. Regenerative air cooling system.

CH-2 SIMPLE VAPOUR COMPRESSION REFRIGERATION SYSTEM

- (i) A ~~vapor~~ VERS is an improved type of air refrigeration system in which a suitable working substance termed as refrigerant is used.
- (ii) Since the low ~~pressure~~ pressure vapour refrigerant from the evaporator is changed high pressure vapour refrigerant in the compressor therefore it is named as vapour compression refrigeration system (VERS).
- (iii) The refrigerants used in this system are ammonia (NH_3), carbon dioxide (CO_2), sulphur dioxide (SO_2).
- (iv) The refrigerant used does not leave the system but it circulates throughout the system alternately condensing and evaporating.
- (v) The vapour compression refrigeration system is now a days used for all purpose refrigeration.
- (vi) It is generally used for industrial purposes from a small domestic refrigerator to a big air conditioning plant.



(Engine - driven vapour compressor heat pump)

Advantages and Disadvantages of VCRS over air refrigeration system:

Advantages :-

- i) It has smaller size for the given capacity of refrigeration.
- ii) It has less running cost.
- iii) It can be employed over a large range of temperature.
- iv) The C.O.P is quite high.

Disadvantages :-

- i) The initial cost is high.
- ii) The prevention of leakage of the refrigerant is the major problem in vapour compression system.

Date: 23/09/2022

Mechanism of SVCRS

1. Compressor :-

The low pressure and temp. vapour refrigerant from evaporator is drawn into compressor through the inlet or suction valve (A), where it is compressed to a high pressure and temperature. That vapour refrigerant is discharged into the condenser through the delivery or discharge valve (B)

2. Condenser :-

The condenser or cooler consist of coils of pipe in which the high pressure and temp. vapour refrigerant is cooled and condensed. The refrigerant while passing through the condenser gives up its latent heat to the surrounding condensing medium which normally air or water

3. Receiver :-

The condensed liquid refrigerant from the condenser is stored in a vessel known as receiver from where it is supply to evaporator through the expansion valve or refrigerant control valve

4. Expansion valve :-

It is also called throttle valve or refrigerant control valve. The function of the expansion-

valve is to allow the liquid refrigerant under high pressure and temperature to pass at a controlled rate after reducing its pressure and temperature. Some of the liquid refrigerant evaporates as it passes through the expansion valve but the greater part is vapourised in the evaporator at low pressure and temperature.

5. Evaporator

An evaporator consists of coils of pipe in which the liquid vapour refrigerant at low temp. & pressure is evaporated and change into vapour refrigerant at low temperature and low pressure.

In evaporating the liquid vapour refrigerant absorbs its latent heat of vapourisation from the medium (Air, water, brine) which is to be cooled

* Brine is used as it has a very low freezing temperature

Types of vapour compression cycle's

1. cycle with dry saturated vapour after compression
2. cycle with wet vapour after compression
3. cycle with superheated vapour after compression
4. cycle with superheated vapour before compression
5. cycle with under cooling or sub cooling of refrigerant.

* Theoretical vapour compression cycle with dry saturated vapour after compression :

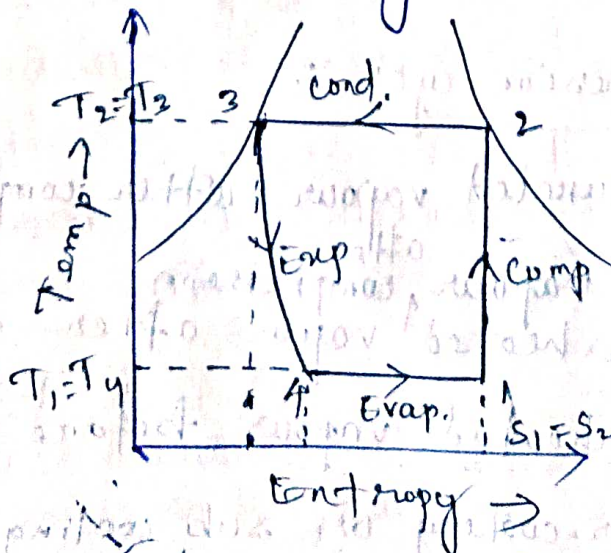
1. Compression process :-

The vapour refrigerant at low pressure P_1 & temperature T_1 is compressed isentropically to dry saturated vapour as shown by vertical line 1-2 on T-s diagram and by curve 1-2 on ~~P-h~~ P-h diagram the pressure & temperature rises from P_1 to P_2 and T_1 to T_2 respectively. The work done during isentropic compression per kg of refrigerant is given by $w = h_2 - h_1$

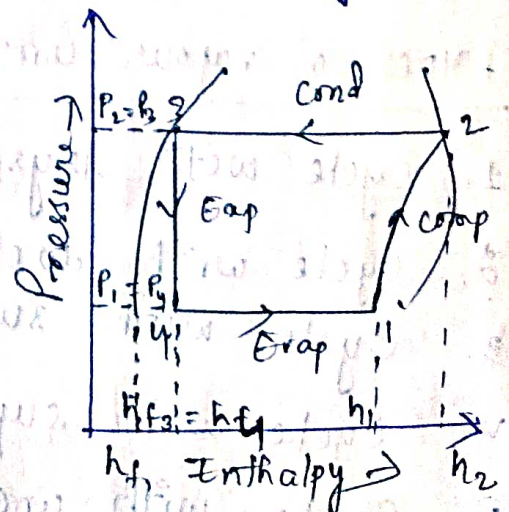
h_1 = Enthalpy of vapour refrigerant at temp. T_1

(at suction of the compressor)

h_2 = Enthalpy of the vapour refrigerant at



(T-s diagram)



(P-h diagram)

2. Condensing process:

The high-pressure and temperature vapour refrigerant from the compressor P_3 passes through the condenser, where it is completely condensed at constant pressure P_2 and temperature T_2 as shown by the ~~curve~~ horizontal line 2-3 on T-s and P-h diagram.

The vapour refrigerant changes into liquid refrigerant. The refrigerant passing through the condenser gives its latent heat to the surrounding condensing medium.

3. Expansion process:

The liquid refrigerant at pressure $P_3 = P_2$ and temperature $T_3 = T_2$ is expanded by throttling process through the expansion valve to a low pressure $P_4 = P_1$ and temperature $T_4 = T_1$ as shown by the curve 3-4 on T-s and P-h diagram.

We have already discussed that some of the liquid refrigerant as it passes through the expansion valve but the greater portion is vapourised in the evaporator. We know that during the throttling process, no heat is absorbed or rejected by the liquid refrigerant.

Note: In case of expansion cylinder ~~is used~~ P_3 is used in place of throttle or expansion valve to expand the liquid refrigerant.

then the ~~the~~ refrigerant will expand isentropically as shown by the dotted vertical line on $T-s$ diagram.

→ The isentropic expansion reduces the external work being expended in running the compressor and increases the refrigerating effect. Thus, the net result of using the expansion cylinder is to increase the C.O.P.

→ Modern domestic refrigerators, capillary is used in place of expansion valve.

4. Vapourising process

→ The liquid vapour mixture at constant temperature $T_4 = T_1$ and pressure $P_4 = P_1$ is evaporated and change into the vapour refrigerant at constant pressure and temp, as shown by horizontal line 4-1 on $T-s$ diagram and $P-h$ diagram.

→ During evaporation the liquid vapour refrigerant absorbs its latent heat of vapourisation from the medium (air, water, brine) which is to be cooled.

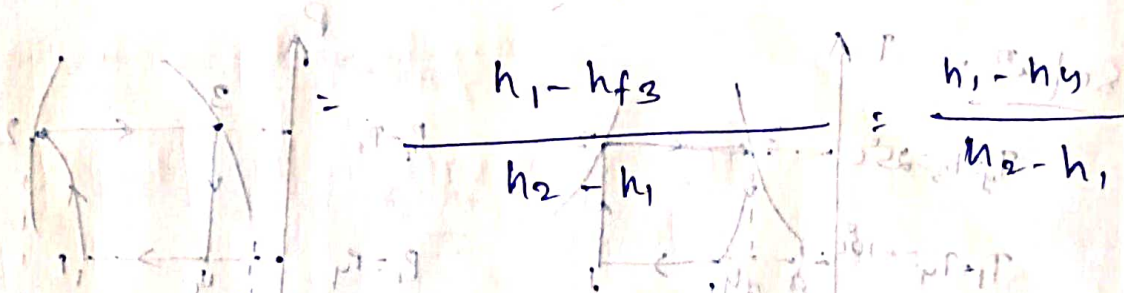
→ This heat which is absorbed by the refrigerant is called refrigerating effect (R_E).

We know that the refrigerating effect or heat absorbed or ~~reject~~ extracted by the liquid vapour refrigerant during evaporation per kg of refrigerant is given by

$$R_e = h_1 - h_4 = h_1 - h_{f3} \quad (\because h_4 = h_{f3})$$

where, h_{f3} = sensible heat at temp. T_3 i.e. enthalpy of liquid refrigerant leaving condenser.

$$\text{C.O.P} = \frac{\text{Refrigeration effect}}{\text{Work done}}$$

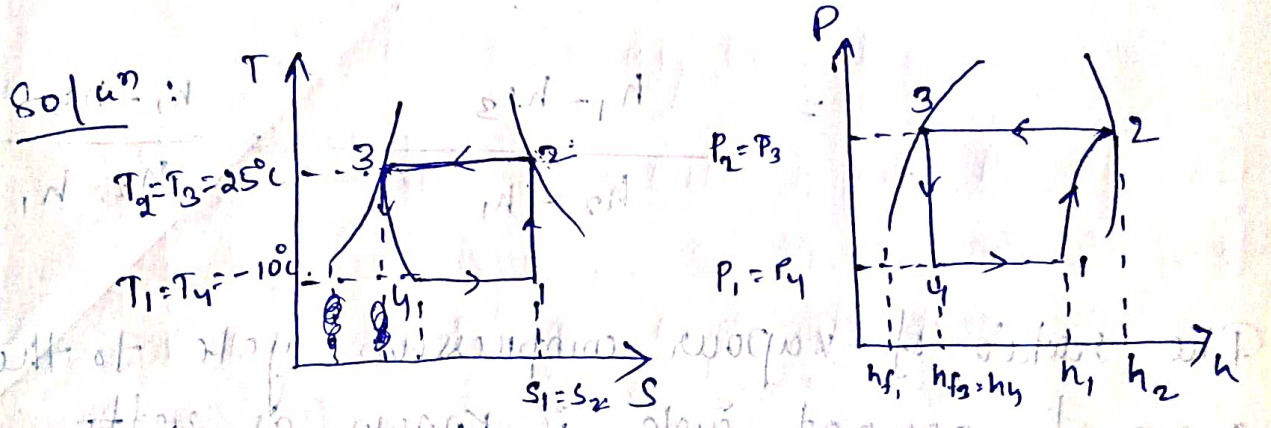


The ratio of vapour compression cycle to the C.O.P of Carnot cycle is known as ~~ratio~~ refrigeration effect (R) or performance index (PI)

~~Ratio~~

Ques The temperature limits of an ammonia refrigeration system are 25°C and -10°C . If the gas is dry at the end of compression calculate the C.O.P. of the cycle assuming no under cooling of the liquid ammonia. Use the following table for the properties of ammonia.

Temp ($^{\circ}\text{C}$)	Liquid heat	Latent heat	liquid entropy
25°C	298.9	1166.94	1.1242
-10°C	135.37	1297.68	0.5443



Given data; $T_2 = T_3 = 25^{\circ}\text{C} = 25 + 273 = 298\text{ K}$
 $T_1 = T_4 = -10^{\circ}\text{C} = -10 + 273 = 263\text{ K}$

$h_{f2} = 298.9\text{ KJ/Kg}$
 $h_{fg2} = 1166.94\text{ KJ/Kg}$
 $s_{f2} = 1.1242\text{ KJ/Kg}$
 $h_{f1} = 135.37\text{ KJ/Kg}$

$$h_{fg1} = 1297.68 \text{ KJ/Kg}$$

$$s_{f1} = 0.5443 \text{ KJ/KgK}$$

Let x_1 = dryness fraction at point 1

We know that entropy at point 1

$$\begin{aligned} s_1 &= s_{f1} + \frac{x_1 h_{fg1}}{T} \\ &= 0.5443 + x_1 \times \frac{1297.68}{263} \\ &= 0.5443 + 4.934 x_1 \quad \text{--- (i)} \end{aligned}$$

Entropy at point 2

$$\begin{aligned} s_2 &= s_{f2} + \frac{h_{fg2}}{T_2} \\ &= 1.1242 + \frac{1166.94}{298} \\ &= 5.04 \text{ KJ/KgK} \quad \text{--- (ii)} \end{aligned}$$

We know that

$$s_1 = s_2$$

$$\Rightarrow 0.5443 + 4.934 x_1 = 5.04$$

$$\Rightarrow x_1 = \frac{5.04 - 0.5443}{4.934} = 0.911$$

Enthalpy at point 1

$$h_1 = h_{f1} + x_1 h_{fg1}$$

$$= 135.37 + 0.910 \times 1297.68$$

$$= ~~1316.25~~ \text{ KJ/Kg}$$

$$= 1316.25 \text{ KJ/Kg}$$

$$h_2 = h_{f2} + h_{fg2}$$

$$= 298.9 + 1166.94$$

$$= 1465.84 \text{ KJ/Kg}$$

$$h_3 = h_{f3} + h_{fg3}$$

$$= h_{f3} = 298.9 \text{ KJ/Kg} = h_{f2} = h_4$$

$$= h_{f3} = 298.9 \text{ KJ/Kg} = h_{f2} = h_4$$

$$\therefore \text{C.O.P} = \frac{\text{Refrigeration effect}}{\text{work done}}$$

$$= \frac{h_1 - h_4}{h_2 - h_1}$$

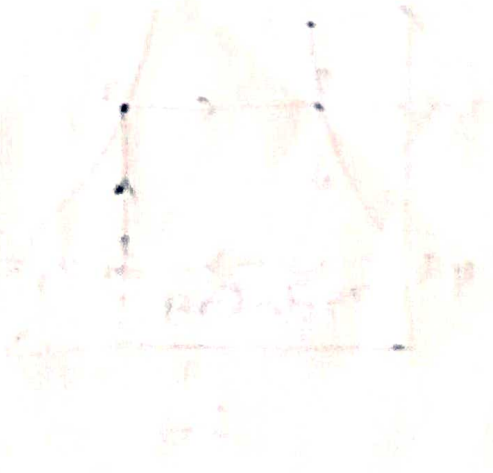
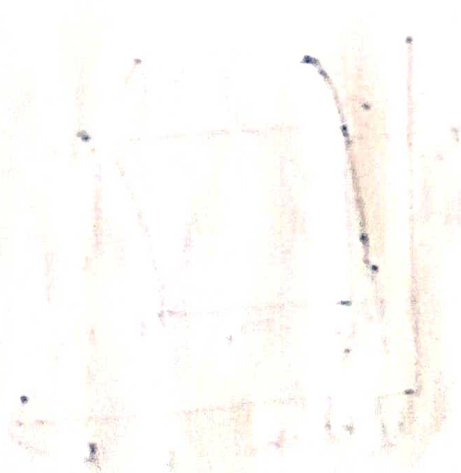
$$= \frac{1316.25 - 298.9}{1465.84 - 1316.25}$$

$$= \frac{1017.35}{149.59}$$

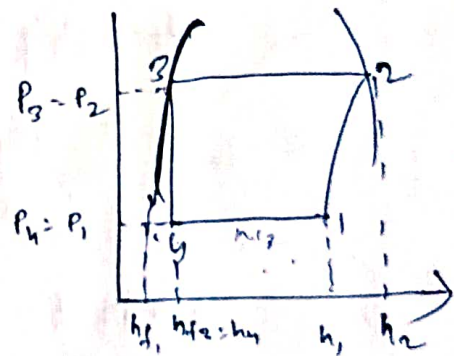
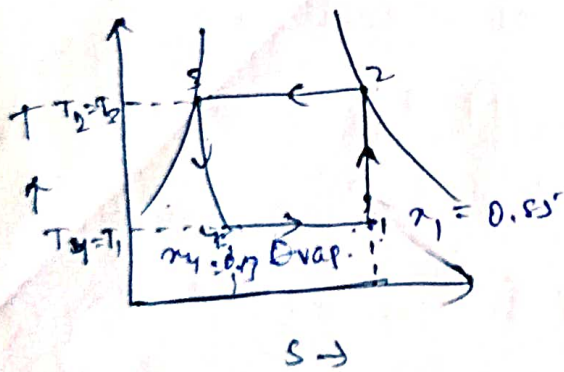
$$= 6.8$$

(Ans)

$$h_{fg} = \text{latent heat of gas}$$



Ques In an ammonia vapour compression system the pressure in the evaporator is 2 bar. Ammonia at exit is 0.85 dry and at entry its dryness fraction is 0.19. During compression the work done per kg of ammonia is 150 kJ. Calculate the C.O.P and the volume of the vapour entering the compressor per minute. If the rate of ammonia circulation is 4.5 kg/min. The latent heat and the specific volume at 2 bar are 1325 kJ/kg and 0.58 m³/kg respectively.



Solⁿ

Given data;

$$P_4 = P_1 = 2 \text{ bar}$$

$$x_1 = 0.85, \quad x_4 = 0.19$$

$$W = 150 \text{ kJ/kg}$$

$$h_{fg} = 1325 \text{ kJ/kg}$$

$$v = 0.58 \text{ m}^3/\text{kg}$$

$$m_a = 4.5 \text{ kg/min}$$

$$\textcircled{1} \text{ C.O.P} = \frac{h_1 - h_4}{W}$$

Let, Enthalpy at point 1

$$h_1 = x_1 \times h_{fg} = 0.85 \times 1325 = 1126.25$$

Enthalpy at point 4 KJ/kg

$$h_4 = x_4 \times h_{fg} = 251.75 \text{ KJ/kg}$$

$$\therefore RE = h_1 - h_4 = 1126.25 - 251.75 = 874.5 \text{ KJ/kg}$$

$$\therefore \text{C.O.P} = \frac{h_1 - h_4}{w} = \frac{1126.25 - 251.75}{150}$$

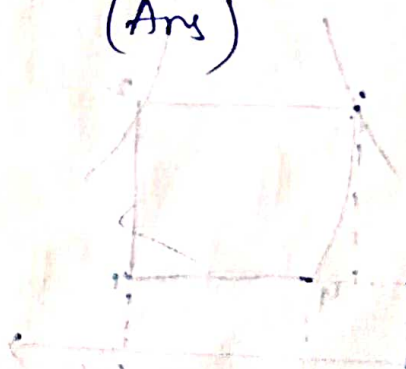
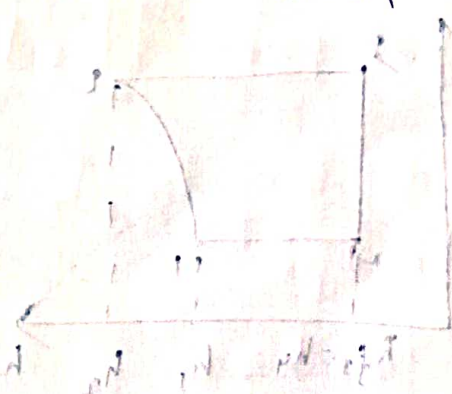
$$= 5.83 \quad (\text{Ans})$$

② Volume of the vapour

$$= M \times \text{specific volume}$$

$$= 4.5 \text{ kg/min} \times 0.58 \text{ m}^3/\text{kg}$$

$$= 2.61 \text{ m}^3/\text{min} \quad (\text{Ans})$$



Theoretical cycle with wet vapour compression

Q. Find the theoretical COP for a CO₂ machine working between the temp. range of 25°C and -5°C. The dryness fraction ~~of~~ of CO₂ gas during the suction stroke is 0.6. Following properties of CO₂ are given

$$h_{f3} = h_{f2} = 164.77 \text{ KJ/kg}$$

$$h_{f1} = h_{f4} = 72.57 \text{ KJ/kg}$$

$$s_{f2} = 0.5978 \text{ KJ/kgK}$$

$$s_{f1} = 0.2862 \text{ KJ/kgK}$$

$$h'_2 = 282.23 \text{ KJ/kg}$$

$$h'_1 = 321.33 \text{ KJ/kg}$$

$$s'_{2'} = 0.9918 \text{ KJ/kgK}$$

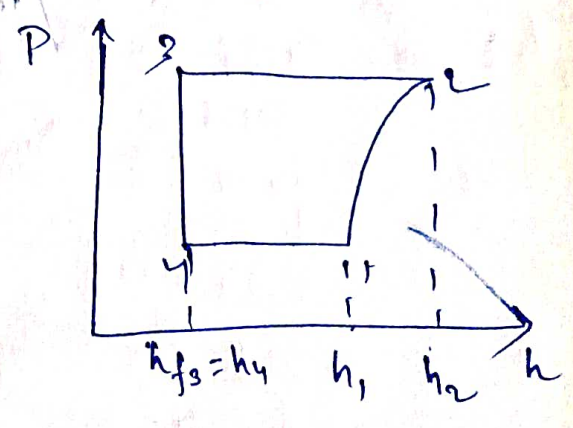
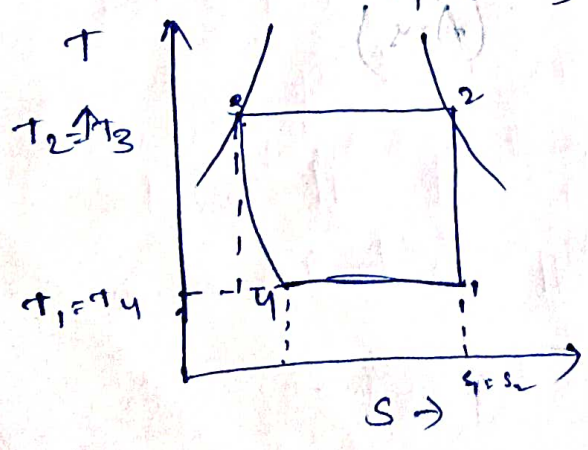
$$s'_1 = 1.2146 \text{ KJ/kgK}$$

$$h_{fg2} = 117.46 \text{ KJ/kg}$$

$$h_{fg1} = 248.76 \text{ KJ/kg}$$

$$T_2 = 25^\circ\text{C} = 25 + 273 = 298 \text{ K}$$

$$T_1 = -5^\circ\text{C} = -5 + 273 = 268 \text{ K}, \alpha_1 = 0.6$$



$$s_2 = s_{f2} + x_2 \frac{h_{fg2}}{T_2}$$

$$= 0.5978 + x_2 \frac{117.46}{298}$$

$$= 0.5978 + 0.394 x_2$$

$$s_1 = s_{f1} + x_1 \frac{h_{fg1}}{T_1}$$

$$= 0.2862 + 0.6 \times \frac{248.76}{268}$$

$$= 0.84$$

We know that

$$s_1 = s_2 \Rightarrow 0.84 = 0.5978 + 0.394 x_2$$

$$x_2 = \frac{0.84 - 0.5978}{0.394} = 0.62$$

$$h_1 = h_{f1} + x_1 h_{fg1}$$

$$= 72.57 + 0.6 \times 248.76 = 221.82 \text{ kJ/kg}$$

$$h_2 = h_{f2} + x_2 h_{fg2} = 164 + 0.62 \times 117.46$$

$$= 236.93 \text{ kJ/kg}$$

$$\therefore \text{Theoretical C.O.P} = \frac{h_3 - h_4}{h_2 - h_1}$$

$$= \frac{221.82 - 164.77}{236.93 - 221.82}$$

$$= 3.77 \quad \text{Ans}$$

Theoretical vapour compression cycle with wet vapour after compression:

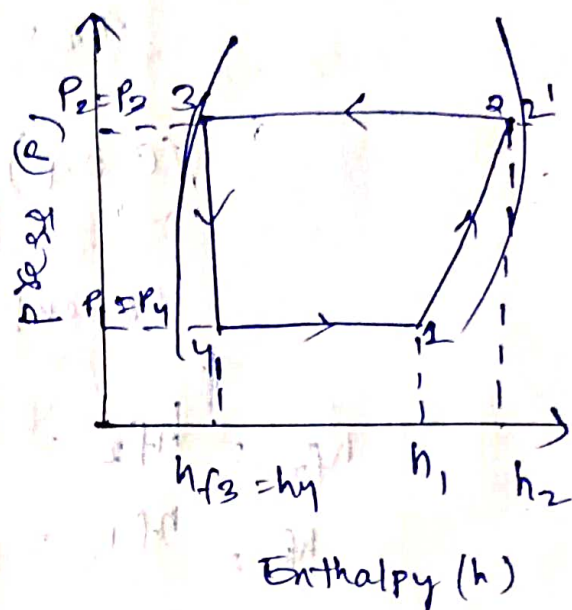
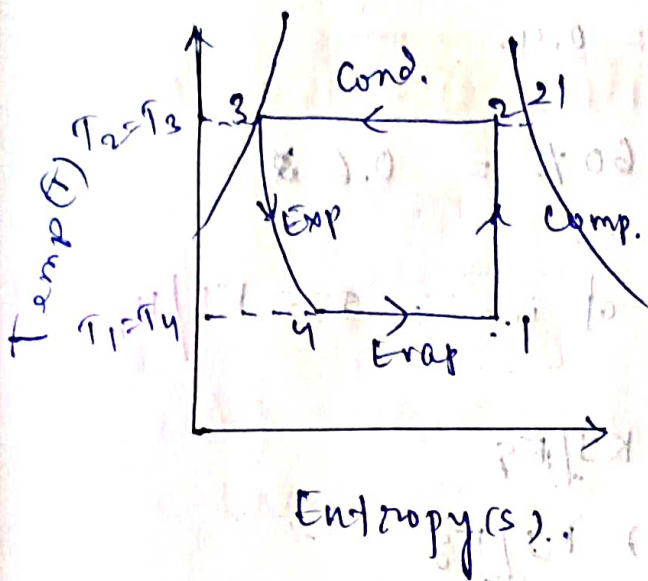
A vapour compression cycle with wet vapour compⁿ is a similar kind of cycle to dry saturated vapour after compression. But in this cycle enthalpy at point 2' found out with the help of dryness fraction at this point. The dryness fraction at point 1 and 2 may be obtained by equating entropies at point 1 and 2.

Now the theoretical C.O.P may be found out as usual from the relation

$$\text{Theoretical C.O.P} = \frac{h_1 - h_2}{h_2 - h_1}$$

$$= \frac{\text{Refrigeration effect}}{\text{Work done}}$$

The T-s and P-h diagram of wet vapour compⁿ is drawn below



$\frac{90}{100}$

Ques An ammonia refrigeration machine filled with an expansion valve works between the temperature limits -10°C and 30°C . the vapour is 95% dry at the end of the isentropic compression & the fluid leaving the condenser is at 30°C assuming actual C.O.P as 60% of theoretical C.O.P calculate the kgs of ice produce per kWhour at 0°C from water at 10°C . Latent heat of ice is 335 KJ/Kg

Temp ($^{\circ}\text{C}$)	Liquid heat (h_f) KJ/Kg	Latent heat (h_{fg}) KJ/Kg	Liquid entropy (s_f)	Total Entropy of d.s.v
30	323.8	1145.80	1.2037	4.9842
-10	135.82	1297.68	0.5443	5.4770

Given data; $T_1 = T_4 = -10^\circ\text{C} = -10 + 273 = 263\text{ K}$

$T_2 = T_3 = 30^\circ\text{C} = 30 + 273 = 303\text{ K}$

$\alpha_2 = 95\% = 0.95$

$(\text{C.O.P})_{\text{act}} = 60\% = 0.6$

Latent heat of ice = 335 KJ/Kg

$h_{f3} = h_{f2} = 323.8\text{ KJ/Kg}$

$h_{g1} = h_{g1} = 135.87\text{ KJ/Kg}$

$h_{fg2} = 1145.80\text{ KJ/Kg}$

$h_{fg1} = 1279.68\text{ KJ/Kg}$

$s_{f2} = 1.2097\text{ KJ/KgK}$

$s_{g1} = 0.5442\text{ KJ/KgK}$

$s'_2 = 4.9842\text{ KJ/KgK}$

$s'_1 = 5.4770\text{ KJ/KgK}$

Let dryness fraction at point (1) be x_1

$s_1 = s_{g1} + \frac{x_1 h_{fg1}}{T_1}$

$= 0.5442 + \frac{x_1 \cdot 1279.68}{263}$

$= 0.5442 + 4.865 x_1$

$$S_2 = \frac{Sf_2 + a_2 hfg_2}{T_2}$$

$$= \frac{1.2037 + 0.95 \times 1145.80}{303}$$

$$= 4.796$$

we know that

$$\Rightarrow 0.5443 + 4.865 a_1 = 4.796$$

$$\Rightarrow a_1 = \frac{4.796 - 0.5443}{4.865}$$

$$h_1 = hf_1 + a_1 hfg_1$$

$$= 135.87 + 0.87 \times 1279.00 = 1249.919$$

$$h_2 = hf_2 + a_2 hfg_2$$

$$= 323.8 + 0.95 \times 1145.80 = 1412.31$$

$$\begin{aligned} \text{Theoretical c.o.p} &= \frac{h_1 - h_2}{h_2 - h_1} \\ &= \frac{1249.19 - 323.8}{1412.31 - 1249.19} \\ &= 5.6 \end{aligned}$$

$$\text{Actual c.o.p} = 0.6 \times 5.6 = 3.36 \quad (\text{Ans})$$

work to be spent corresponding to 1 kW hr

$$W = 3600 \text{ KJ}$$

∴ Actual heat extracted or ref. effect

$$\text{Per kW hour} = W \times (\text{COP})_{\text{act}}$$

$$= 3600 \times 3.36$$

$$= 12096 \text{ KJ}$$

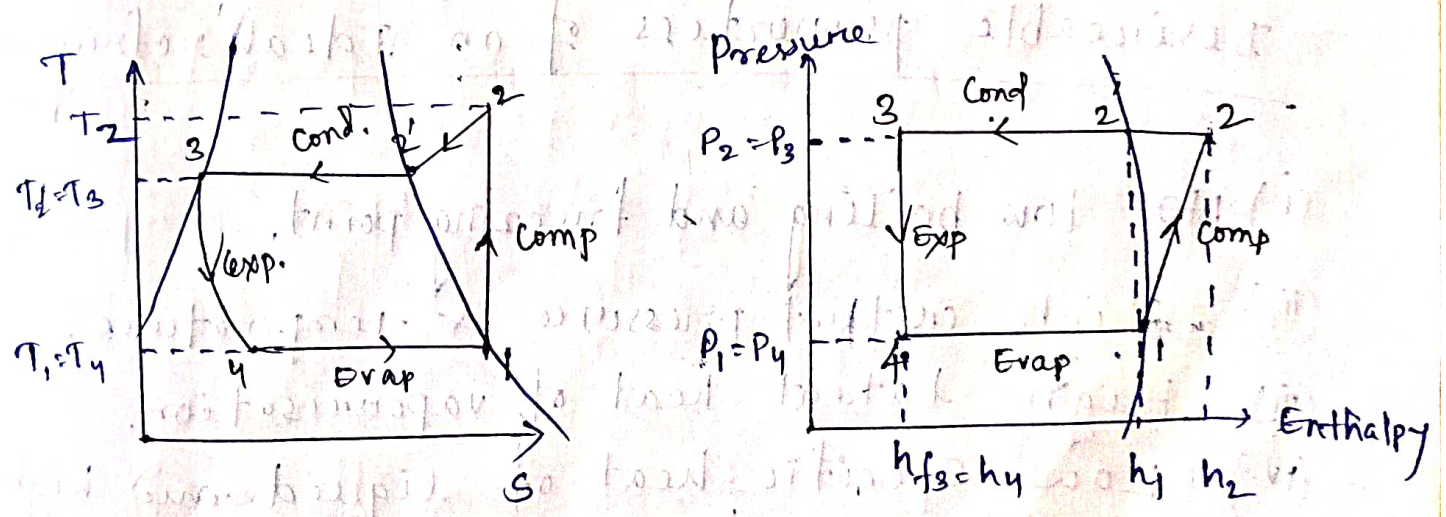
We know that

Theoretical vapour compression ~~refrigeration~~ ^{Cycle} system with superheated vapour ~~before~~ ^{after} compression.

In this cycle the enthalpy at point 2 is found out with the help of degree of super heat. The degree of super heat may be found out by equating the entropies at point 1 and 2. Now the C.O.P may be found out as usual from the relation

$$C.O.P = \frac{\text{Refrigeration effect}}{\text{Work done}}$$

$$= \frac{h_1 - h_{f3}}{h_2 - h_1}$$



A little consideration will show that the super heating increases the refrigerating effect and the amount of work done in the compressor. since the increase in refrigeration effect is less as compare to, increase in work done therefore the net effect of super heating is to have low C.O.P

In this cycle the cooling of ^{superheated} vapour ~~to~~ will take place in two stages.

→ Firstly it will be condensed to dry saturated stage as constant pressure (shown by graph 2-2') and second it will be condensed at constant temp (shown by graph 2'-3). The remaining is same as discussed in wet vapour after compression

* Refrigerant :

Desireable properties of an Ideal refrigerant

(i) ~~NO~~: low boiling and freezing point.

(ii) High critical pressure & temperature.

(iii) High latent heat of vapourisation.

(iv) Low specific heat of liquid and high specific heat of vapour.

(v) Low specific volume of vapour.

(vi) High thermal conductivity.

(vii) Non corrosive to metal.

(viii) Non flame-able and non-explosive.

(ix) Non toxic

- (x) Low cost.
- (xi) Easily and regularly available
- (xii) Easy to liquefy and moderate pressure & temperature
- (xiii) Easy of locating leaks and by odour or suitable indicator.
- (xiv) Miscible with oil.
- (xv) High COP.
- (xvi) Ozone friendly

The standard compression of refrigerant, as used in the refrigeration industry is based on an evaporating temperature of -15°C and a condensing temperature of $+30^{\circ}\text{C}$.

CLASSIFICATION OF REFRIGERANTS :

The refrigerants may be broadly classified as into the following two groups:

- ① Primary refrigerants and;
- ② Secondary refrigerants.

The primary refrigerants which is directly take part in the refrigeration system are called primary refrigerants, whereas the refrigerants which are first cooled by primary refrigerants and then used for cooling purpose are known as secondary refrigerants.

VAPOUR ABSORPTION REFRIGERATION SYSTEM

- The vapour absorption refrigeration system is one of the oldest method of producing refrigeration effect.
- The system may be used in both domestic & large Industries refrigerating plant.
- The refrigerant that used in vapour absorption system is ammonia.
- The vapour absorption system uses the heat energy instead of mechanical energy as in vapour compression system in order to change conditions of the refrigerant required for the operations of the refrigeration cycle.
- In VARS, the compressor is replaced by an vapour absorber, a pump, a generator & a pressure reducing valve. These components in VARS perform the same function as that of a compressor in RCS.
- The vapour refrigerant from the evaporator is drawn into an absorber where it is absorbed by the weak solution of the refrigerant forming a strong refrigerant solution.
- The strong solution is pumped to the generator where it is heated by some external source. During the heating process the vapour refrigerant

is driven off by the solution and enters into the condenser where it is liquified. The liquid refrigerant then flows into the evaporator and thus the cycle is completed.

SIMPLE VAPOUR ABSORPTION SYSTEM:

→ List of vapour absorption system components :-
an absorber, a pump, a generator, a pressure reducing valve, condenser, receiver, expansion valve, evaporator.

→ The low pressure ammonia vapour leaving the evaporator enters the absorber where it is absorbed by the cold water in the absorber. The water has the ability to absorb very large quantities of ammonia vapour and their solution thus, formed, is known as AQUA-AMMONIA.

→ The absorption of ammonia water lowers the pressure in the absorber which in turn draws more ammonia vapour from the evaporator and thus rises the temp of solution.

→ Some form of cooling arrangement (usually water cooling) is employed in the absorber to remove the heat of solution evolved there.

→ This is necessary in order to increase the absorption capacity of water, because of higher temperature water absorber less ammonia vapour.

→ The strong solution thus formed in the absorber is pumped to the generator by the liquid pump. The pump increases the pressure of the solution up to 10 bar.

→ The strong solution of ammonia in the generator is heated by some external source such as gas or steam.

→ During the heating process, the ammonia vapour is driven off the solution at high pressure leaving behind the hot weak ammonia solution in the ammonia.

→ This weak solution of ammonia flows back to the absorber at low pressure after passing through the pressure reducing valve.

→ The high pressure ammonia vapour from the generator is condensed in the condenser to a high pressure liquid ammonia.
→ This liquid ammonia is passed to the expansion valve through the receiver and then to the evaporator. This completes the simple vapour absorption cycle.

Refrigerant:

Refrigerant is a heat carrying medium which during their cycle in the refrigeration system absorb heat from a low temperature system and discard the heat to a higher temperature system surrounding.

Properties of refrigerant :

- (i) Low boiling point
- (ii) High critical temperature
- (iii) High latent heat of vapourisation
- (iv) Low specific heat of liquid and
- (v) Low specific volume of vapour
- (vi) Non corrosive to metal
- (vii) Non-flameable and non explosive
- (viii) Non-toxic
- (ix) Low cost.
- (x) Easy to liquify at moderate pressure and temperature.
- ~~(xi) Easy to leaks, by~~
- ~~(xii) Easy of locating.~~

- (vi) Easy of locating by leaks by odour or suitable indicator.
- (vii) Mixes well with oil.

Classification of refrigerant :-

1. Primary refrigerant
2. Secondary refrigerant.

1. Primary refrigerant :-

The primary refrigerants directly take part in the refrigeration system are called primary refrigerants.

2. Secondary ref. :-

The secondary ref. are first cooled by primary refrigerant then used for cooling purposes are known as secondary refrigerants.

Primary refrigerant types :-

Primary refrigerants are following 4 groups

1. Halo carbon refrigerant
2. Azeotrope ref.
3. Inorganic ref.
4. Hydro carbon ref.

① Halocarbons

The American Society of Heating Refrigeration and Air-Conditioning Engineers (ASHRAE).

Identify 42-Halocarbon compounds as refrigerants. These are all synthetically produced.

Ex -

<u>Ref. No</u>	<u>Chemical name</u>	<u>Chm formula</u>
R-11	Trichloromethane - Methane	CCl_3F (23.77°C)
R-12	Dichlorodifluoromethane	CCl_2F_2 (-29°C)
R-22	Monochloro	

Azeotrope:

The term azeotrope refers to a stable mixture of refrigerants whose vapour & liquid phases worked identical compositions over a wide range of temperature.

Ex: R-500 \rightarrow 73.8% R-12 + 26.2% R-152

R-502 \rightarrow 48.8% R-22 + 51.2% R-152

Inorganic ref.

The inorganic refrigerants were exclusively used before the introduction of halocarbon refrigerants.

Ex: R-717 \rightarrow NH_3 \rightarrow Ammonia \rightarrow B.P \rightarrow 33.3°C

R-729 \rightarrow Air \rightarrow

R-744 \rightarrow CO_2 \rightarrow B.P \rightarrow -73.6°C

R-764 \rightarrow SO_2 \rightarrow

R-118 \rightarrow Water (H_2O) \rightarrow

Used in air craft refrigeration system.

CO_2 \rightarrow

SO_2 \rightarrow Used in house hold and small commercial system.

H_2O \rightarrow Used for refrigerant vapour in absorption system.

Hydro carbons

It's are successfully used in industrial & commercial installations. They possess satisfactory thermodynamic properties but are highly flammable and explosive.

R-170 \rightarrow ethane \rightarrow C_2H_6

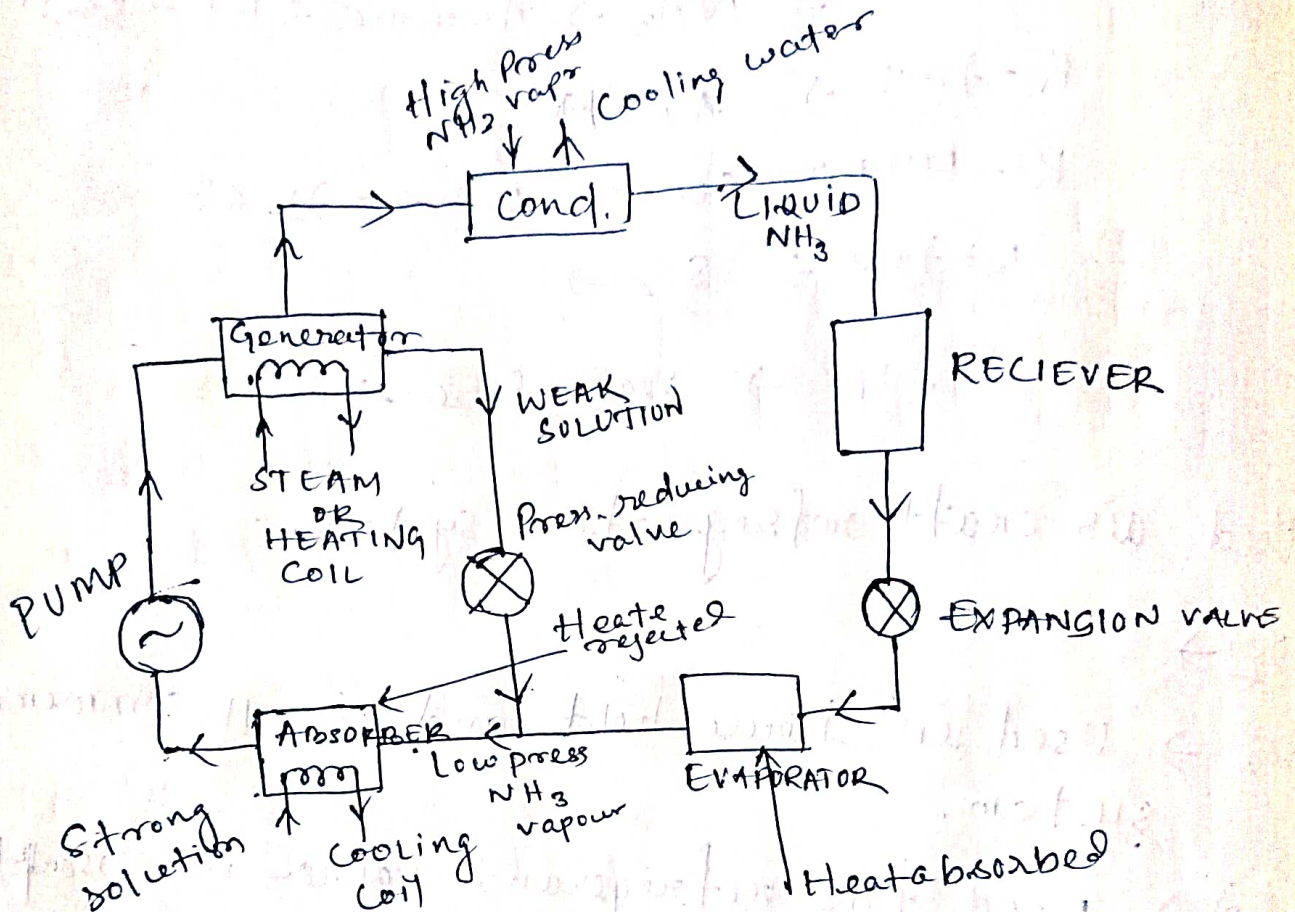
R-290 \rightarrow Propane \rightarrow C_3H_8

R-1150 \rightarrow Ethylene \rightarrow C_2H_4

R - 600 \rightarrow Butane \rightarrow C_4H_{10}

Date: 25/11/2023

(CH-3) VAPOUR ABSORPTION SYSTEM



It is one of the oldest method of producing refrigeration effect. It may be used in both the domestic and large industrial refrigerating plants. NH_3 is commonly used the vapour absorption system uses heat energy, instead of mechanical energy as in vapour compression system.

In this system the vapour refrigerant from the evaporator is drawn into the absorber where it is absorbed by weak solution the refrigerant forming a strong solution. This strong solution is pumped to the generator where it is heated by some external source then it is entered into the condenser where it is liquified.

(CH-5)

AIR-CONDITIONING SYSTEM

The air conditioning is a branch of engineering which deals with the study of conditioning of air i.e. supplying and maintaining desirable internal atmospheric conditions for human comfort, irrespective of external conditions.

It also deals with conditioning of air for industrial purposes, food preserving, storage of food and other materials.

Factor effecting for comfort air-conditioning:

1. Temperature of air:

It may be noted that a human being feels comfortable when the air is at 21°C with 56% relative humidity.

2. Humidity of air:

In general for summer air conditioning, the relative humidity should be less than 60%. Where as for winter air conditioning it should not be 40%.

3. Purity of air:

For the comfort of a human-body proper filtration, cleaning and purification of air is essential to keep it free from dust and other impurities.

4. Motion of air:

The motion of air circulation is another important factor which should be controlled in order to keep constant temperature the condition space.

water 28/11
difference between air cooled and water cooled condenser.

Air cooled Condenser

The construction of air cooled cond. is very simple thus the initial cost is less.

No handling problem
Air cooled condenser donot required piping arrangement for carrying the air

there is no problem in disposing of used air

Since there is no corrosion therefore fouling effect is low

Water cooled condenser

(i) The construction of water cooled condenser is complicated, thus the initial cost is high

(ii) Difficult to handle

(iii) water cooled condenser required piping arrangement

(iv) There is a problem of disposing the use water unless a recirculation system is provided.

(v) since corrosion occurs inside the tube carrying the water, therefore fouling effects are high.

(vi) The air cooled condensers have low heat transfer capacity

(vii) The fan noise is high

(viii) These condensers have high flexibility

(ix) The distribution of air on condensing surface is non-uniform.

(vi) The water cooled condensers have high heat transfer capacity

(vii) There is no fan noise

(viii) These condensers have low flexibility.

(ix) The distribution of water on condensing surface is uniform.

Classification of compressors:

1. According to method of compression

a) Reciprocating compressors

b) Rotary compressors

c) Centrifugal compressor

2. According to number of strokes:

a) single acting compressors

b) Double acting compressors.

3. According to number of stages:

a) single stage compressors

b) Multi stage compressors.

4. According to drive

- a) Direct drive compressors
- b) Belt drive compressors.

According to location of prime mover

- a) Semi hermetic compressor (Direct drive, motor and compressor in separate housings)
- b) Hermetic compressor (Direct drive, motor and compressor in the same housing)

Ques Define swept volume.

→ It is also known as stroke volume or piston displacement volume.

→ It is the volume swept by the piston when it moves from top or inner dead position to bottom or outer dead position.

$$V_p = \frac{\pi}{4} \times D^2 \times L$$

Psychometric terms:

1. Dry air:

→ A pure dry air is a mixture of number of gases such as nitrogen, oxygen, carbon dioxide, hydrogen, Argon, Neon, Helium etc.

- The pure dry air does not ordinarily exist because it always contains some water vapour
- The density of dry air is taken as 1.293 Kg/m^3 at pressure 1.0135 bar and at temperature 0°C

2. Moist air:

- It is a mixture of dry air and water vapour. The amount of water vapour present in the air depends upon the absolute pressure and temperature of the mixture

3. Saturated air:-

- It is a mixture of dry air and water vapour, when the air has diffused maximum water vapour. The water vapours usually occur in the form of superheated steam.
- When the saturated air is cooled, the water vapour in the air starts condensing and are visible in the form of moist air, fog or condensation on cold surfaces

4. Degree of saturation:

It is the ratio of actual mass of water vapour in a unit mass of dry air to the mass of

water vapour in the same mass of dry air when it is saturated at the same temperature

Date: 30/11/2022

Dry Bulb Temp

The temperature of air measured by ordinary thermometer is known as dry bulb temp. of the air

Wet Bulb temperature

The temperature of air measured by a thermometer when its bulb is covered with weight wet cloth is exposed to a current of air is known as wet bulb temperature.

Note: The difference between DBT & WBT is known as wet bulb depression. Wet bulb depression will be zero when the air becomes saturated.

Dew point temperature:

It is defined as the temperature at which the moisture present in the air begins to condense when the air is cooled. The dew point temperature corresponds to the —

Saturation temperature of water vapour in the mixture of air and wet vapour

- The dry-bulb, wet bulb and dew point temperature will all be say for saturated air

Specific Humidity %

It is the mass of water vapour present in one Kg of dry air.

Absolute Humidity:

The mass of water vapour present in $1m^3$ of air is known as Absolute Humidity.

Degree of saturation:

It is defined as the ratio of water vapour in unit mass of dry air when it is saturated.

Relative Humidity:

It is equal to the ratio of actual mass of water vapour in a given volume of moist air to the mass of water vapour of the saturated air at the same temp

Psychometric :

The science which deals with the study of the behaviour of air and water vapour mixture is known as psychometry.

The properties of water vapour and air mixture are known as psychometric properties.

What is the function of rectifier in VARS

In case the ^{water} vapours are not completely removed in the analysis, a closed type vapour cooler called rectifier is used. It is generally water cooled and may be of the double pipe, shell and coil, or shell and tube type. Its function is to cool further the ammonia vapours leaving the analyser so that the remaining water vapours are condensed thus only dry ammonia vapours flow to the condenser.

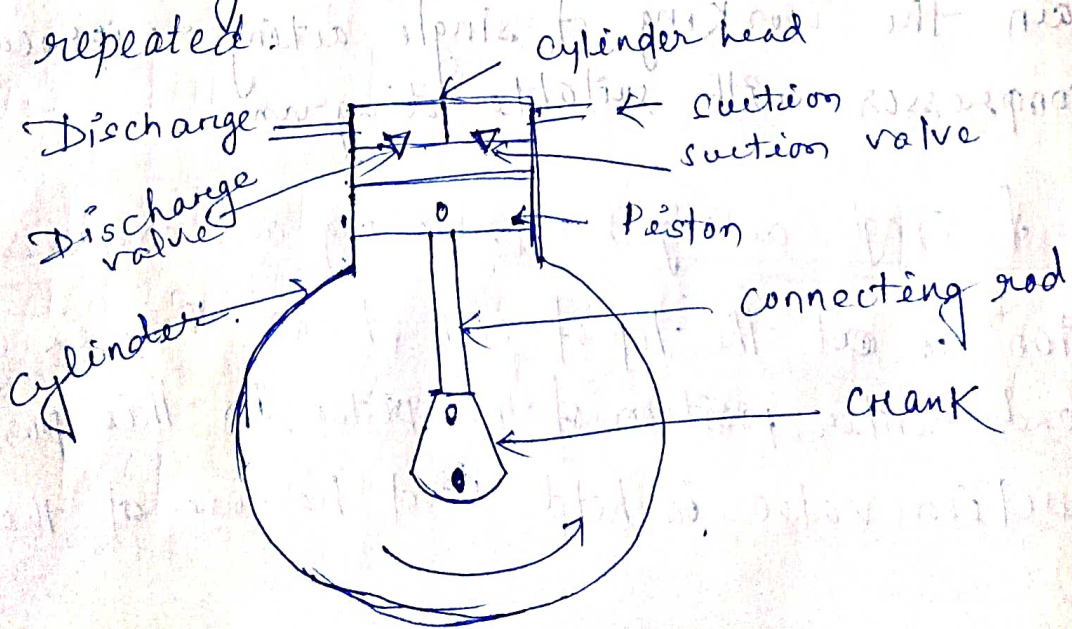
Ques Explain the working of single acting reciprocating air compressor with suitable diagram.

Working of single acting reciprocating air compressor :

The piston is at the top of each stroke this is called Top dead center position of the piston. In this position the suction valve is held closed because of the -

Pressure in the clearance space between the top of the piston and the cylinder head. The discharge valve is also ~~held~~ held closed because of the cylinder head pressure acting on the top of it.

→ When the piston moves downward, the refrigerant left in the clearance space expands. Thus the volume of the cylinder above the piston increases and the pressure inside the cylinder decreases. When the pressure becomes slightly less than the suction pressure or atmospheric pressure, the suction valve gets open and the vapour refrigerant flows in the cylinder. This flow continues until the piston reaches the bottom of the stroke. Here the suction valve closes. Now when the piston moves upward the volume of cylinder decreases and the pressure inside the cylinder increases. When the pressure inside the cylinder becomes greater than that on the top of the discharge valve, the discharge valve gets open and the vapour refrigerant is discharged into the condenser and the cycle is repeated.



Cold storage plant:

A cool store or cold store is a large refrigerated room or building designed for storage of goods in an environment below the outer temperature.

Many food products may be stored at some temp. above the freezing point. The storage may be ^{short term} storage or long term storage. The storages which are used for short term storage purposes are known as cold storages. The short term storage is usually meant for written establishment where rapid turnover of the product is expected. The period for short term storage ranges from one to two days or to a week but not more than 15 days. The long term storage is usually carried out by wholesalers and commercial storage ware houses. The storage period depends on the type of products stored and its condition on entering the storage. The maximum storage period for long term storage ranges from 10 days for sensitive products like ripe tomatoes and upto 6 to 8 months for more durable products such as onions. When perishable fruits are to be stored for longer period, they should be frozen and stored in frozen storages.

The conditions required for short term storages are more flexible than those required for long term storage.

→ Following points should be kept in mind while storing the foods in cold storages.

1. Storage temperature
2. Relative humidity and air motion
3. Mined storage
4. Condition of products at the time of entering storage
5. Product chilling

Ques What are the materials used for constructing duct in an air conditioning system?

1. Galvanised iron sheet metal
2. Aluminium sheet metal
3. Black steel
4. Resin bonded glass fibre
5. Cement asbestos duct for underground air distribution.
6. wooden ducts

Air filter function :-

The function of air filter is to arrest the solid impurities such as soot, ash, smoke fumes & even living organisms such as viruses, bacteria & fungus

Classification of Air filter:

1. Dry air filter
2. Viscous Impingement filter
3. Electrostatic filters

P-v diagram and t-s diagram of reversed Carnot cycle:

